

Comparative Study of Population Forecasting Methods

Dinesh W. Gawatre¹, Mahesh H. Kandgule², Shankar D. Kharat²

¹(Asst. professor, Civil Engineering Department, Sinhgad Academy of Engineering, Pune)

²(Student, Civil Engineering Department, Sinhgad Academy of Engineering, Pune)

Abstract: Precise calculation of population contributes in various aspects of providing facilities to the public. In civil engineering, many structures like sewage treatment plant, water treatment plant, sizes of reservoirs, storage tanks etc., are dependant upon the future population of the area for a specific design period. more or less the population than the actual population if taken it may hamper the project objective. Therefore one need to figure out accurately the population of desired span of years. The report has been prepared to compare the various population forecasting methods.

Keywords: census, decade, incremental, logistic, population.

I. Introduction

India is the second most populous country in the world. And the rate of increase in population is also high. It indicates the need of precise calculation of the future population. For the successful design of the structures related to public use on a larger scale there is need to consider the most probable future population. Inaccurate or unsuitable methods of the population forecasting when used may result in increased cost of the construction or unable to satisfy the the project requirements. There are various methods used for forecasting the population each assuming various factors and assumptions. Each method gives the different value of future population. An attempt is made in this paper to compare the population of Pune district of year 2011 with the calculated population of the same year by five different methods. The populations of year 1971 to year 2001 were taken for calculation purpose. The population of Pune district consisted of populations of the villages and small towns even involved in the district. So no method is perfectly suitable for the conditions.

II. Methods Of Population Forecasting

Following are the commonly used methods for forecasting-

- 1) Arithmetic increase method
- 2) Geometric increase method
- 3) Incremental increase method
- 4) Simple graphical method
- 5) The logistic curve method

1) Arithmetic increase method:-

Average rate of increase in population is assumed to be constant from decade to decade in this method. Average increase per decade is found out from the previously available census data. The product of this amount obtained and number of decades for which the population is to be worked out is added to the present population of the subjected area to get the approximate population after n decades.

$$P_n = P + nd$$

Where, P_n = future population after n decades

P = present population

n = number of decades

d = average increase per decade

Year	Population in Lakh
1971	31.78
1981	41.64
1991	55.33
2001	72.32

Sr.No	Year	Population in Lakh	Increase in Population
1	1971	31.78	-
2	1981	41.64	09.86
3	1991	55.33	13.69
4	2001	72.32	16.99
Total			40.54

Solution:-

For calculating the population of 2011,

$$\text{No. of decades (n)} = \frac{2011-2001}{10} = 1$$

$$P_o = 72.32$$

$$\text{Average increase in decade(d)} = \frac{40.54}{3} = 13.5133$$

$$\text{Population at the end of 2011 (P}_n) = P_o + nd$$

$$P_n = 72.32 + (1 \times 13.5133) = 85.8333 \text{ lakh}$$

2) Geometric increase method

Average percentage increase in population is assumed to be constant from decade to decade in this method. Average percentage increase per decade is found out from the previously available census data. By using the formula given below the future population is worked out.

$$P_n = P \left(1 + \frac{r}{100} \right)^n$$

Where, P_n = future population after n decades

P = present population

n = number of decades

r = average percentage increase per decade

Year	Population in Lakh	Increase in population	Percentage increase in population
1971	31.78	-	-
1981	41.64	9.86	$\frac{9.86 \times 100}{31.78} = 31.025$
1991	55.33	13.69	$\frac{13.69 \times 100}{41.64} = 32.877$
2001	72.32	16.99	$\frac{16.99 \times 100}{55.33} = 30.706$
Total		40.54	94.608
Avg percentage decade		$\frac{40.54}{3} = 13.5133$	$\frac{94.608}{3} = 31.536$

Average percentage increase (r) = 31.536%

$$\text{No. of decades (n)} = \frac{2011-2001}{10} = 1$$

$$P_o = 72.32$$

$$\text{Population at the end of 2011 (P}_n) = P \left(1 + \frac{r}{100} \right)^n$$

$$P_n = 72.32 \left(1 + \frac{31.536}{100} \right)^1$$

$$P_n = 95.1268 \text{ lakh}$$

3) Incremental increase method

The advantages of both arithmetic increase method and geometrical increase method are included in this method. Average increase per decade is found out first of all and average percentage increase per decade is worked out as in arithmetic increase method and geometric increase method respectively. Future population is worked out from the equation given below.

$$P_n = P + nd + \frac{n(n+1)}{2} t$$

Where, P_n = future population after n decades

P = present population

n = number of decades

t = average incremental increase per decade

d = average increase per decade

Year	Population in Lakh	Increase in population	Incremental increase
1971	31.78	-	-
1981	41.64	9.86	-
1991	55.33	13.69	+3.83
2001	72.32	16.99	+3.3
Total		40.54	+7.13
Avg percentage decade		$\frac{40.54}{3} = 13.5133$	$T = 3.565$

$$\text{No. of decades } (n) = \frac{2011-2001}{10} = 1$$

$$P_0 = 72.32$$

$$\text{Population at the end of 2011 } (P_n) = P + nd + \frac{n(n+1)}{2}t$$

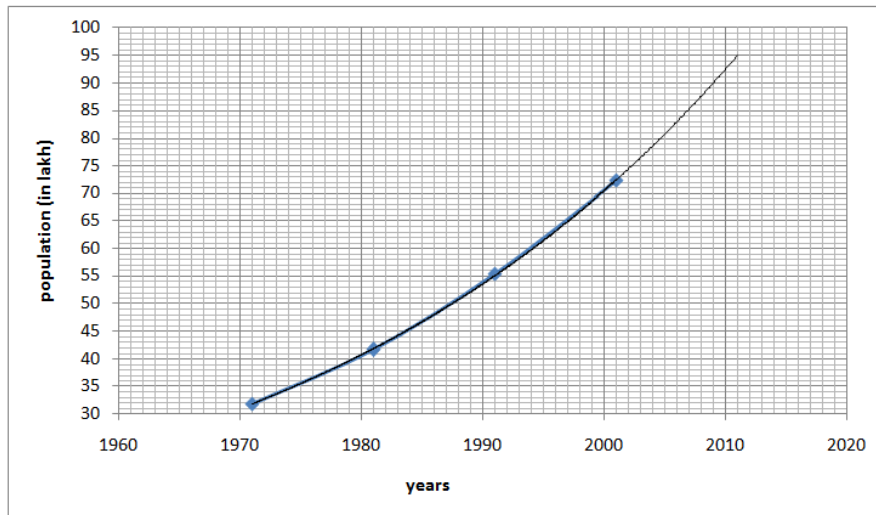
$$(P_n) = 72.32 + 1(13.5133) + \frac{1(1+1)}{2}3.565$$

$$(P_n) = 89.3983 \text{ lakh}$$

4) Simple graphical method

Graph between the population and the corresponding year is plotted based on the available census data. The obtained curve is extended in the same manner to get the population of required year. It is the approximate method as the accuracy is dependent on the skill and experience of the person dragging the curve.

Year	Population in Lakh
1971	31.78
1981	41.64
1991	55.33
2001	72.32



From graph, population at the end of 2011 = 95.00 lakh

5) The logistic curve method

The growth is assumed to be a function of the time and follows some logical mathematical relationship the population tends to according to the logistic curve starting at low rate followed by high rate and then at lower rate towards the saturation limit.

Year	Population in Lakh
1971	31.78
1981	41.64
1991	55.33
2001	72.32

$$P_0 = 41.64, t_0 = 0$$

$$P_1 = 55.33, t_1 = 10 \text{ years}$$

$$P_2 = 72.32, t_2 = 20 \text{ years}$$

The saturation population can be calculated by using equation

$$P_s = \frac{2P_0P_1P_2 - (P_1^2(P_0 + P_2))}{P_0P_2 - P_1^2}$$

$$P_s = \frac{2 \times 41.64 \times 55.33 \times 72.32 - (55.33^2(41.64 + 72.32))}{41.64 \times 72.32 - 55.33^2} = 312.6964$$

$$\text{We have, } m = \frac{P_s - P_0}{P_0} = \frac{312.6964 - 41.64}{41.64} = 6.5095$$

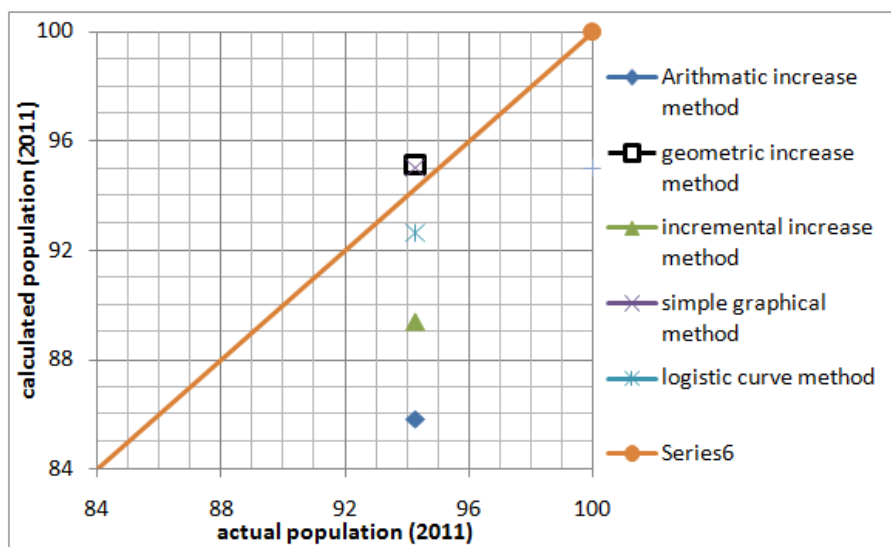
$$n = \left(\frac{2.303}{t^1}\right) \log_{10} \frac{P_0(P_s - P_1)}{P_1(P_s - P_0)} = \left(\frac{2.303}{10}\right) \log_{10} \frac{41.64(312.6964 - 55.33)}{55.33(312.6964 - 41.64)} = -0.0336$$

Population in 2011

$$P = \frac{P_s}{1 + m \log e^{-1}(n.t)} = \frac{312.6964}{1 + 6.5095 \log e^{-1}(-0.0336 \times 30)} = 92.633 \text{ lakh}$$

Percentage error in calculation

Sr.no.	method	Actual population of 2011	Calculated population of 2011	Percentage error
1.	Arithmetical increase method	94.29	85.8333	8.96
2.	Geometrical increase method	94.29	95.1268	0.88
3.	Incremental increase method	94.29	89.3983	5.18
4.	Simple graphical method	94.29	95.000	0.75
5.	Logistic curve method	94.29	92.633	1.756



III. Conclusion

In the Light of the above, we can see that the geometric increase method is a simple realistic population model based on past information. This method tends to give a higher estimate than normal since it behaves exponentially. It more accurately describes the continuous and cumulative nature of population growth.

From the above graph and table it is concluded that the error of calculation of future population lies within the ± 10%. The geometrical increase method is found to be the most accurate method calculation of the future population as simple graphical method is subjected to various errors.

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