

bT-Locally Closed Sets and bT-Locally Continuous Functions In Supra Topological Spaces.

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Abstract: The aim of this paper is to introduce a decompositions namely supra bT- locally closed sets and define supra bT-locally continuous functions. This paper also discussed some of their properties.

Keyword S-BTLC set, S-BTL- continuous, S-BTL- irresolute.

I. Introduction

In 1983 Mashhour et al [8] introduced Supra topological spaces and studied S- continuous maps and S^* - continuous maps. In 2011, Bharathi.S[3] introduced and investigated several properties of generalization of locally b- closed sets. In 1997, Arokiarani .I[2] introduced and investigated some properties of regular generalized locally closed sets and RGL-continuous functions. In this paper, we define a new set called supra bT- locally closed and also define supra bT- locally continuous functions and investigated some of the basic properties for this class of functions.

II. Preliminaries

Definition 2.1[8,10] A subfamily of μ of X is said to be a supra topology on X, if

- (i) $X, \phi \in \mu$
- (ii) if $A_i \in \mu$ for all $i \in J$ then $\cup A_i \in \mu$.

The pair (X, μ) is called supra topological space. The elements of μ are called supra open sets in (X, μ) and complement of a supra open set is called a supra closed set.

Definition 2.2[10] (i) The supra closure of a set A is denoted by $cl^\mu(A)$ and is defined as $cl^\mu(A) = \cap \{B : B \text{ is a supra closed set and } A \subseteq B\}$.

(ii) The supra interior of a set A is denoted by $int^\mu(A)$ and defined as $int^\mu(A) = \cup \{B : B \text{ is a supra open set and } A \supseteq B\}$.

Definition 2.3[8] Let (X, τ) be a topological spaces and μ be a supra topology on X. We call μ a supra topology associated with τ if $\tau \subset \mu$.

Definition 2.4[10] Let (X, μ) be a supra topological space. A set A is called a supra b-open set if $A \subseteq cl^\mu(int^\mu(A)) \cup int^\mu(cl^\mu(A))$. The complement of a supra b-open set is called a supra b-closed set.

Definition 2.5[7] A subset A of a supra topological space (X, μ) is called bT^μ-closed set if $bcl^\mu(A) \subseteq U$ whenever $A \subseteq U$ and U is T^μ- open in (X, μ) .

Definition 2.6[9] Let A and B be subsets of X. Then A and B are said to be supra separated, if $A \cap cl^\mu(B) = B \cap cl^\mu(A) = \phi$.

Definition 2.7[5] Let $(X, \tau) \rightarrow (Y, \sigma)$ be two topological spaces and $\tau \subseteq \mu$. A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called supra continuous, if the inverse image of each open set of Y is a supra open set in X.

Definition 2.8[6] Let $(X, \tau) \rightarrow (Y, \sigma)$ be two topological spaces and μ and λ be supra topologies associated with τ and σ respectively. A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called supra irresolute, if $f^{-1}(A)$ is supra open set of X for every supra open set A in Y.

Notations

S-BTLC* denotes supra bT* - locally closed set and S-BTLC** denotes supra bT** - locally closed set.

III. SUPRA bT-LOCALLY CLOSED SETS

Definition 3.1

Let (X, μ) be a supra topological space. A subset A of (X, μ) is called supra bT – locally closed set, if $A = U \cap V$, where U is supra bT – open in (X, μ) and V is supra bT – closed in (X, μ) . The collection of all supra bT- locally closed set S of X will be denoted by $S\text{-BTLC}(X)$.

Remark 3.2

Every supra bT-closed set (resp. supra bT- open set) is $S\text{-BTLC}$.

Definition 3.3

For a subset A of supra topological space (X, μ) , $A \in S\text{-BTLC}^*(X, \mu)$, if there exist a supra bT- open set U and a supra closed set V of (X, μ) , respectively such that $A = U \cap V$.

Remark 3.4

Every supra bT-closed set (resp. supra bT-open set) is $S\text{-BTLC}^*$.

Definition 3.5

For a subset A of supra topological space (X, μ) , $A \in S\text{-BTLC}^{**}(X, \mu)$, if there exist a supra open set U and a supra bT - closed set V of (X, μ) , respectively such that $A = U \cap V$.

Remark 3.6

Every supra bT-closed set (resp. supra bT-open set) is $S\text{-BTLC}^{**}$.

Theorem 3.7 Let A be a subset of (X, μ) . If $A \in S\text{-BTLC}^*(X, \mu)$ (or) $S\text{-BTLC}^{**}(X, \mu)$ then A is $S\text{-BTLC}(X, \mu)$.

Proof Given $A \in S\text{-BTLC}^*(X, \mu)$ (or) $S\text{-BTLC}^{**}(X, \mu)$, by definition $A = U \cap V$, where U is supra bT- open set and V is supra closed set (or) U is supra open set and V is supra bT – closed set. By theorem 3.2 [7] every supra closed set is supra bT – closed set, therefore V is supra bT – closed set (or) every supra open set is supra bT – closed set, therefore U is supra bT- open set. Then A is $S\text{-BTLC}(X, \mu)$.

Example 3.8

Let $X = \{a, b, c\}$ and $\mu = \{X, \emptyset, \{a\}, \{b\}, \{a, b\}\}$. In this (X, μ) , $S\text{-BTLC}^*(X, \mu)$ and $S\text{-BTLC}^{**}(X, \mu)$ are the proper subset of $S\text{-BTLC}(X, \mu)$, because $S\text{-BTLC}(X, \mu) = P(X)$.

Theorem 3.9 Let A be a subset of (X, μ) . If $A \in S\text{-LC}(X, \mu)$ then A is $S\text{-BTLC}(X, \mu)$.

Proof Given $A \in S\text{-LC}$, by definition $A = U \cap V$, where U is supra open set and V is supra closed set. Since every supra open set is supra bT – open set and every supra closed set is supra bT – closed set. Then $A \in S\text{-BTLC}(X, \mu)$

The converse of the above theorem is not true from the following example.

Example 3.10

Let $X = \{a, b, c\}$ and $\mu = \{X, \emptyset, \{a\}\}$. $S\text{-LC}(X, \mu) = \{X, \emptyset, \{a\}, \{b, c\}\}$ and $S\text{-BTLC}(X, \mu) = P(X)$.

Theorem 3.11 For a subset A of (X, μ) , the following are equivalent:

- (i) $A \in S\text{-BTLC}^{**}(X, \mu)$
- (ii) $A = U \cap \text{bcl}^\mu(A)$, for some supra open set U
- (iii) $\text{bcl}^\mu(A) - A$ is supra bT- closed
- (iv) $A \cup [X - \text{bcl}^\mu(A)]$ is supra bT- open

Proof (i) \Rightarrow (ii): Given $A \in S\text{-BTLC}^{**}(X, \mu)$, then there exist a supra open subset U and a supra bT- closed subset V such that $A = U \cap V$. Since $A \subset U$ and $A \subset \text{bcl}^\mu(A)$, then $A \subset U \cap \text{bcl}^\mu(A)$.

Conversely, we have $\text{bcl}^\mu(A) \subset V$ and hence $A = U \cap V \supset U \cap \text{bcl}^\mu(A)$. Therefore $A = U \cap \text{bcl}^\mu(A)$.

(ii) \Rightarrow (i): Let $A = U \cap \text{bcl}^\mu(A)$, for some supra open set U . Clearly, $\text{bcl}^\mu(A)$ is supra bT- closed and hence $A = U \cap \text{bcl}^\mu(A) \in S\text{-BTLC}^{**}(X, \mu)$.

(ii) \Rightarrow (iii): Let $A = U \cap \text{bcl}^\mu(A)$, for some supra open set U . Then $A \in S\text{-BTLC}^{**}(X, \mu)$. This implies U is supra open and $\text{bcl}^\mu(A)$ is supra bT – closed. Therefore $\text{bcl}^\mu(A) - A$ is supra bT- closed.

(iii) \Rightarrow (ii): Let $U = X - [\text{bcl}^\mu(A) - A]$. By (iii) U is supra bT- open in X . We know that every supra open is supra bT- open, therefore U is supra open in X . Then $A = U \cap \text{bcl}^\mu(A)$ holds.

(iii) \Rightarrow (iv): Let $Q = \text{bcl}^\mu(A) - A$ be supra bT – closed. Then $X - Q = X - [\text{bcl}^\mu(A) - A] = A \cup [X - \text{bcl}^\mu(A)]$. Since $X - Q$ is supra bT – open, $A \cup [X - \text{bcl}^\mu(A)]$ is supra bT – open.

(iv) \Rightarrow (iii): Let $U = A \cup [X - \text{bcl}^\mu(A)]$. Since $X - U$ is supra bT – closed and $X - U = \text{bcl}^\mu(A) - A$ is supra bT – closed.

Definition 3.12

Let A be subset of (X, μ) . Then

- (i) The supra bT-closure of a set A is denoted by $\text{bT-cl}^\mu(A)$, define as $\text{bT-cl}^\mu(A) = \bigcap \{B : B \text{ is supra bT-closed and } A \subseteq B\}$.

(ii) The supra bT-interior of a set A is denoted by $bT\text{-int}^\mu(A)$, define as $bT\text{-int}^\mu(A) = \bigcap \{B : B \text{ is supra bT-open and } B \subseteq A\}$.

Theorem 3.13 For a subset A of (X, μ) , the following are equivalent:

- (i) $A \in S\text{-BTLC}(X, \mu)$
- (ii) $A = U \cap bT\text{-cl}^\mu(A)$, for some supra bT - open set U
- (iii) $bT\text{-cl}^\mu(A) - A$ is supra bT- closed
- (iv) $A \cup [X - bT\text{-cl}^\mu(A)]$ is supra bT- open

Proof (i) \Rightarrow (ii): Given $A \in S\text{-BTLC}(X, \mu)$, then there exist a supra bT - open subset U and a supra bT-closed subset V such that $A = U \cap V$. Since $A \subseteq U$ and $A \subseteq bT\text{-cl}^\mu(A)$, then $A \subseteq U \cap bT\text{-cl}^\mu(A)$.

Conversely, we have $bT\text{-cl}^\mu(A) \subseteq V$ and hence $A = U \cap V \supseteq U \cap bT\text{-cl}^\mu(A)$. Therefore $A = U \cap bT\text{-cl}^\mu(A)$.

(ii) \Rightarrow (i): Let $A = U \cap bT\text{-cl}^\mu(A)$, for some supra bT - open set U. Clearly, $bT\text{-cl}^\mu(A)$ is supra bT- closed and hence $A = U \cap bT\text{-cl}^\mu(A) \in S\text{-BTLC}(X, \mu)$.

(ii) \Rightarrow (iii): Let $A = U \cap bT\text{-cl}^\mu(A)$, for some supra bT - open set U. Then $A \in S\text{-BTLC}(X, \mu)$. This implies U is supra bT - open and $bT\text{-cl}^\mu(A)$ is supra bT - closed. Therefore $bT\text{-cl}^\mu(A) - A$ is supra bT- closed.

(iii) \Rightarrow (ii): Let $U = X - [bT\text{-cl}^\mu(A) - A]$. By (iii) U is supra bT- open in X. Then $A = U \cap bT\text{-cl}^\mu(A)$ holds.

(iii) \Rightarrow (iv): Let $Q = bT\text{-cl}^\mu(A) - A$ be supra bT - closed. Then $X - Q = X - [bT\text{-cl}^\mu(A) - A] = A \cup [X - bT\text{-cl}^\mu(A)]$. Since X-Q is supra bT - open, $A \cup [X - bT\text{-cl}^\mu(A)]$ is supra bT -open.

(iv) \Rightarrow (iii): Let $U = A \cup [X - bT\text{-cl}^\mu(A)]$. Since X-U is supra bT - closed and $X - U = bT\text{-cl}^\mu(A) - A$ is supra bT - closed.

Theorem 3.14 For a subset A of (X, μ) , the following are equivalent:

- (i) $A \in S\text{-BTLC}^*(X, \mu)$
- (ii) $A = U \cap cl^\mu(A)$, for some supra bT - open set U
- (iii) $bcl^\mu(A) - A$ is supra bT- closed
- (iv) $A \cup [X - bcl^\mu(A)]$ is supra bT- open

Proof (i) \Rightarrow (ii): Given $A \in S\text{-BTLC}^*(X, \mu)$, then there exist a supra bT - open subset U and a supra closed subset V such that $A = U \cap V$. Since $A \subseteq U$ and $A \subseteq cl^\mu(A)$, then $A \subseteq U \cap cl^\mu(A)$.

Conversely, we have $cl^\mu(A) \subseteq V$ and hence $A = U \cap V \supseteq U \cap cl^\mu(A)$. Therefore $A = U \cap cl^\mu(A)$.

(ii) \Rightarrow (i): Let $A = U \cap cl^\mu(A)$, for some supra bT - open set U. Clearly, $cl^\mu(A)$ is supra closed and hence $A = U \cap cl^\mu(A) \in S\text{-BTLC}^*(X, \mu)$.

(ii) \Rightarrow (iii): Let $A = U \cap cl^\mu(A)$, for some supra bT - open set U. Then $A \in S\text{-BTLC}^*(X, \mu)$. This implies U is supra bT - open and $cl^\mu(A)$ is supra closed. Therefore $cl^\mu(A) - A$ is supra closed. We know that every supra closed is supra bT- closed, therefore $bcl^\mu(A) - A$ is supra bT - closed.

(iii) \Rightarrow (ii): Let $U = X - [bcl^\mu(A) - A]$. By (iii) U is supra bT- open in X. Then $A = U \cap cl^\mu(A)$ holds.

(iii) \Rightarrow (iv): Let $Q = bcl^\mu(A) - A$ be supra bT -closed. Then $X - Q = X - [bcl^\mu(A) - A] = A \cup [X - bcl^\mu(A)]$. Since X- Q is supra bT - open, $A \cup [X - bcl^\mu(A)]$ is supra bT - open.

(iv) \Rightarrow (iii): Let $U = A \cup [X - bcl^\mu(A)]$. Since X-U is supra bT -closed and $X - U = bcl^\mu(A) - A$ is supra bT - closed.

Theorem 3.15 For a subset A of (X, μ) , if $A \in S\text{-BTLC}^{**}(X, \mu)$, then there exist an supra open set G such that $A = G \cap bT\text{-cl}^\mu(A)$.

Proof Let $A \in S\text{-BTLC}^{**}(X, \mu)$. Then $A = G \cap V \Rightarrow A \subseteq G$. Then $A \subseteq bT\text{-cl}^\mu(A)$. Therefore, $A \subseteq G \cap bT\text{-cl}^\mu(A)$. Also, we have $bT\text{-cl}^\mu(A) \subseteq V$. This implies $A = G \cap V \supseteq G \cap bT\text{-cl}^\mu(A) \Rightarrow A \supseteq G \cap bT\text{-cl}^\mu(A)$. Thus $A = G \cap bT\text{-cl}^\mu(A)$.

Theorem 3.16 For a subset A of (X, μ) , if $A \in S\text{-BTLC}^{**}(X, \mu)$, then there exist an supra open set G such that $A = G \cap bcl^\mu(A)$.

Proof Let $A \in S\text{-BTLC}^{**}(X, \mu)$. Then $A = G \cap V$, where G is supra open set and V is supra bT-closed set. Then $A = G \cap V \Rightarrow A \subseteq G$. Obviously, $A \subseteq bcl^\mu(A)$.

Therefore, $A \subseteq G \cap bcl^\mu(A)$. -----(1)

Also, we have $bcl^\mu(A) \subseteq V$. This implies $A = G \cap V \supseteq G \cap bcl^\mu(A) \Rightarrow A \supseteq G \cap bcl^\mu(A)$.------(2)

From (1) and (2), we get $A = G \cap bcl^\mu(A)$.

Theorem 3.17 Let A be a subset of (X, μ) . If $A \in S\text{-BTLC}^{**}(X, \mu)$, then $bT\text{-cl}^\mu(A) - A$ is supra bT- closed and $A \cup [X - bT\text{-cl}^\mu(A)]$ is supra bT - open.

Proof Given $A \in S\text{-BTLC}^{**}(X, \mu)$. Then there exist a supra open subset U and a supra bT- closed subset V such that $A = U \cap V$. This implies $bT\text{-cl}^\mu(A)$ is supra bT- closed. Therefore, $bT\text{-cl}^\mu(A) - A$ is supra bT- closed. Also, $[X - [bT\text{-cl}^\mu(A) - A]] = A \cup [X - bT\text{-cl}^\mu(A)]$. Therefore $A \cup [X - bT\text{-cl}^\mu(A)]$ is supra bT - open.

Remark 3.18 The converse of the above theorem need not be true as seen from the following example.

Example 3.19 Let $X = \{a, b, c, d\}$ and $\mu = (X, \phi, \{a\}, \{b\}, \{a, b\})$. Then $\{X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, c\}, \{a, d\}, \{b, c\}, \{b, d\}, \{c, d\}, \{a, c, d\}, \{b, c, d\}\}$ is the set of all supra bT-closed set in X

and $S\text{-BTLC}^{**}(X, \mu) = P(X) - \{\{a, b, c\}, \{a, b, d\}\}$. If $A = \{a, b, c\}$, then $bT\text{-cl}^{\mu}(A) - A = \{d\}$ is supra bT - closed and $A \cup [X \text{-} bT\text{-cl}^{\mu}(A)] = A$ is supra bT - open but $A \notin S\text{-BTLC}^{**}(X, \mu)$.

Theorem 3.20 If $A \in S\text{-BTLC}^*(X, \mu)$ and B is supra open, then $A \cap B \in S\text{-BTLC}^*(X, \mu)$.

Proof Suppose $A \in S\text{-BTLC}^*(X, \mu)$, then there exist a supra bT - open set U and supra closed set V such that $A = U \cap V$. So $A \cap B = U \cap V \cap B = (U \cap B) \cap V$, where $U \cap B$ is supra bT - open. Therefore, $A \cap B \in S\text{-BTLC}^*(X, \mu)$.

Theorem 3.21 If $A \in S\text{-BTLC}(X, \mu)$ and B is supra open, then $A \cap B \in S\text{-BTLC}(X, \mu)$.

Proof Suppose $A \in S\text{-BTLC}(X, \mu)$, then there exist a supra bT - open set U and supra bT - closed set V such that $A = U \cap V$. So $A \cap B = U \cap V \cap B = (U \cap B) \cap V$, where $U \cap B$ is supra bT - open. Therefore, $A \cap B \in S\text{-BTLC}(X, \mu)$.

Theorem 3.22 If $A \in S\text{-BTLC}^{**}(X, \mu)$ and B is supra closed, then $A \cap B \in S\text{-BTLC}^{**}(X, \mu)$.

Proof Suppose $A \in S\text{-BTLC}^{**}(X, \mu)$, then there exist a supra open set U and supra bT - closed set V such that $A = U \cap V$. So $A \cap B = U \cap V \cap B = U \cap (B \cap V)$, where $B \cap V$ is supra bT - closed. Hence, $A \cap B \in S\text{-BTLC}^{**}(X, \mu)$.

IV. SUPRA bT - LOCALLY CONTINUOUS FUNCTIONS

In this section, we define a new type of functions called supra bT - locally continuous functions ($S\text{-BTL}$ -continuous functions), supra bT - locally irresolute functions ($S\text{-BTL}$ -irresolute) and study some of their properties.

Definition 4.1

Let (X, τ) and (Y, σ) be two topological spaces and $\tau \subseteq \mu$. A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called $S\text{-BTL}$ -continuous (resp., $S\text{-BTL}^*$ - continuous, and $S\text{-BTL}^{**}$ - continuous), if $f^{-1}(A) \in S\text{-BTLC}(X, \mu)$, (resp., $f^{-1}(A) \in S\text{-BTLC}^*(X, \mu)$, and $f^{-1}(A) \in S\text{-BTLC}^{**}(X, \mu)$) for each $A \in \sigma$.

Definition 4.2

Let (X, τ) and (Y, σ) be two topological spaces and μ and λ be a supra topologies associated with τ and σ respectively. A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be $S\text{-BTL}$ -irresolute (resp., $S\text{-BTL}^*$ - irresolute, resp., $S\text{-BTL}^{**}$ -irresolute) if $f^{-1}(A) \in S\text{-BTLC}(X, \mu)$, (resp., $f^{-1}(A) \in S\text{-BTLC}^*(X, \mu)$, resp., $f^{-1}(A) \in S\text{-BTLC}^{**}(X, \mu)$) for each $A \in S\text{-BTLC}(Y, \lambda)$ (resp., $A \in S\text{-BTLC}^*(Y, \lambda)$, resp., $A \in S\text{-BTLC}^{**}(Y, \lambda)$).

Theorem 4.3 Let (X, τ) and (Y, σ) be two topological spaces and μ be a supra topology associated with τ . Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be a function. If f is $S\text{-BTL}^*$ - continuous (or) $S\text{-BTL}^{**}$ - continuous, then it is $S\text{-BTL}$ -continuous.

Proof Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be a function. If f is $S\text{-BTL}^*$ - continuous (or) $S\text{-BTL}^{**}$ - continuous, by definition $f^{-1}(A) \in S\text{-BTLC}^*(X, \mu)$, and $f^{-1}(A) \in S\text{-BTLC}^{**}(X, \mu)$ for each $A \in \sigma$. By theorem 3.7, $f^{-1}(A) \in S\text{-BTLC}(X, \mu)$. Then it is $S\text{-BTL}$ - continuous.

Theorem 4.4 Let (X, τ) and (Y, σ) be two topological spaces and μ and λ be a supra topologies associated with τ and σ respectively. Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be a function. If f is $S\text{-BTL}$ -irresolute (resp., $S\text{-BTL}^*$ - irresolute, and $S\text{-BTL}^{**}$ -irresolute), then it is $S\text{-BTL}$ - continuous (resp., $S\text{-BTL}^*$ - continuous, and $S\text{-BTL}^{**}$ - continuous).

Proof Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be a function. Let A is supra closed of Y . By theorem 3.2[7] every supra closed set is supra bT -closed set, therefore A is supra bT - closed set. Since f is $S\text{-BTL}$ -irresolute (resp., $S\text{-BTL}^*$ - irresolute, and $S\text{-BTL}^{**}$ -irresolute), $f^{-1}(A)$ is $S\text{-BTL}$ -closed. Therefore f is $S\text{-BTL}$ -continuous (resp., $S\text{-BTL}^*$ - continuous, and $S\text{-BTL}^{**}$ - continuous).

Theorem 4.5 If $g: X \rightarrow Y$ is $S\text{-BTL}$ - continuous and $h: Y \rightarrow Z$ is supra continuous, then $h \circ g: X \rightarrow Z$ is $S\text{-BTL}$ -continuous.

Proof Let $g: X \rightarrow Y$ is $S\text{-BTL}$ - continuous and $h: Y \rightarrow Z$ is supra continuous. By definition, $g^{-1}(V) \in S\text{-BTLC}(X)$, $V \in Y$ and $h^{-1}(W) \in Y$, $W \in Z$. Let $W \in Z$, then $(h \circ g)^{-1}(W) = (g^{-1}h^{-1})(W) = g^{-1}(h^{-1}(W)) = g^{-1}(V)$, for $V \in Y$. This implies, $(h \circ g)^{-1}(W) = g^{-1}(V) \in S\text{-BTLC}(X)$, $W \in Z$. Hence $h \circ g$ is $S\text{-BTL}$ - continuous.

Theorem 4.6 If $g: X \rightarrow Y$ is $S\text{-BTL}$ -irresolute and $h: Y \rightarrow Z$ is $S\text{-BTL}$ -continuous, then $h \circ g: X \rightarrow Z$ is $S\text{-BTL}$ - continuous.

Proof Let $g: X \rightarrow Y$ is $S\text{-BTL}$ -irresolute and $h: Y \rightarrow Z$ is $S\text{-BTL}$ -continuous. By definition, $g^{-1}(V) \in S\text{-BTLC}(X)$, for $V \in S\text{-BTLC}(Y)$ and $h^{-1}(W) \in S\text{-BTLC}(Y)$, for $W \in Z$. Let $W \in Z$, then $(h \circ g)^{-1}(W) = (g^{-1}h^{-1})(W) = g^{-1}(h^{-1}(W)) = g^{-1}(V)$, for $V \in S\text{-BTLC}(Y)$. This implies, $(h \circ g)^{-1}(W) = g^{-1}(V) \in S\text{-BTLC}(X)$, $W \in Z$. Hence $h \circ g$ is $S\text{-BTL}$ - continuous.

Theorem 4.7 If $g: X \rightarrow Y$ and $h: Y \rightarrow Z$ are $S\text{-BTL}$ - irresolute, then $h \circ g: X \rightarrow Z$ is $S\text{-BTL}$ - irresolute.

Proof By the hypothesis and the definition, we have $g^{-1}(V) \in S\text{-BTLC}(X)$, for $V \in S\text{-BTLC}(Y)$ and $h^{-1}(W) \in S\text{-BTLC}(Y)$, for $W \in S\text{-BTLC}(Z)$. Let $W \in S\text{-BTLC}(Z)$, then $(hog)^{-1}(W) = (g^{-1}h^{-1})(W) = g^{-1}(h^{-1}(W)) = g^{-1}(V)$, for $V \in S\text{-BTLC}(Y)$. Therefore, $(hog)^{-1}(W) = g^{-1}(V) \in S\text{-BTLC}(X)$, $W \in S\text{-BTLC}(Z)$. Thus, hog is $S\text{-BTL}$ -irresolute.

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