

Some New Models Of Cosmology Other Than Einstein And De Sitter

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Abstract:

This paper explores novel cosmological models that diverge from the traditional Einstein-de Sitter framework. We investigate the theoretical foundations and observational implications of several alternative cosmologies, including the Brans-Dicke theory, Modified Newtonian Dynamics (MOND), and the Conformal Cyclic Cosmology (CCC) model. Through a comprehensive analysis of these models, we aim to shed light on their potential to address current challenges in our understanding of the universe, such as dark matter, dark energy, and the nature of cosmic inflation. Our findings suggest that while these alternative models offer intriguing perspectives on cosmic evolution, they also face significant challenges in reconciling with observational data. This research contributes to the ongoing dialogue in cosmology and highlights the importance of considering diverse theoretical frameworks in our quest to understand the universe.

Keywords: Cosmology, Einstein-de Sitter Model, Brans-Dicke Theory, MOND, Conformal Cyclic Cosmology.

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I. Introduction

The field of cosmology has been dominated by the Lambda-CDM model, which is based on Einstein's General Relativity and incorporates the concepts of dark matter and dark energy. This model, often referred to as the "standard model" of cosmology, has been remarkably successful in explaining a wide range of observational data, from the cosmic microwave background to the large-scale structure of the universe [15].

However, despite its successes, the Lambda-CDM model faces several challenges. These include the nature of dark matter and dark energy, the flatness and horizon problems, and the apparent tension between different measurements of the Hubble constant [7]. These challenges have motivated researchers to explore alternative cosmological models that might provide new insights or solutions to these problems.

This paper focuses on three alternative cosmological models that diverge from the Einstein-de Sitter framework:

1. The Brans-Dicke theory
2. Modified Newtonian Dynamics (MOND)
3. Conformal Cyclic Cosmology (CCC)

Each of these models proposes significant modifications to our understanding of gravity, space-time, or the evolution of the universe. By examining these alternatives, we aim to broaden our perspective on cosmology and potentially uncover new avenues for addressing the current challenges in the field.

The structure of this paper is as follows: Section II provides a brief overview of the Einstein-de Sitter model as a point of reference. Sections III, IV, and V delve into the Brans-Dicke theory, MOND, and CCC, respectively, discussing their theoretical foundations, key predictions, and observational tests. Section VI compares these models with each other and with the standard Lambda-CDM model. Finally, Section VII concludes the paper with a discussion of the implications of these alternative models for our understanding of the universe and suggestions for future research directions.

II. The Einstein De Sitter Model: A Brief Overview

Before delving into alternative cosmological models, it is essential to understand the Einstein-de Sitter model, which serves as a foundation for much of modern cosmology. The Einstein-de Sitter model, proposed by Albert Einstein and Willem de Sitter in 1932, is a particular solution to Einstein's field equations in General Relativity [8].

The model describes a homogeneous, isotropic universe filled with matter and radiation. It assumes a flat spatial geometry and a cosmic scale factor that evolves as a power law with time. The key features of the Einstein-de Sitter model include:

1. Flat geometry ($k = 0$)

2. Matter-dominated universe ($\Omega_m = 1$)
3. No cosmological constant ($\Lambda = 0$)
4. Scale factor evolves as $a(t) \propto t^{2/3}$

The Einstein-de Sitter model provided a simple and elegant description of the universe's evolution. However, observational evidence, particularly from Type Ia supernovae in the late 1990s, revealed that the universe's expansion is accelerating, contradicting the deceleration predicted by the Einstein-de Sitter model [14,16].

This discovery led to the introduction of dark energy and the development of the Lambda-CDM model, which has since become the standard model of cosmology. Despite its limitations, the Einstein-de Sitter model remains an important reference point in cosmology and serves as a useful approximation in certain contexts.

III. The Brans-Dicke Theory

The Brans-Dicke theory, proposed by Carl Brans and Robert Dicke in 1961, is one of the earliest and most well-known alternatives to Einstein's General Relativity [5]. It is a scalar-tensor theory of gravity that introduces a scalar field ϕ in addition to the metric tensor $g_{\mu\nu}$ of General Relativity.

A. Theoretical Foundation

The Brans-Dicke theory is based on Mach's principle, which suggests that the inertial mass of an object is determined by the distribution of matter in the universe. In this theory, the gravitational constant G is not a fundamental constant but is determined by the scalar field ϕ , which can vary in space and time.

The action for the Brans-Dicke theory is given by:

$$S = \int d^4x \sqrt{-g} \left[\phi R - \omega \frac{\partial_\mu \phi \partial^\mu \phi}{\phi} + L_m \right]$$

Where:

- R is the Ricci scalar
- ω is the Brans-Dicke parameter
- L_m is the matter Lagrangian

The field equations derived from this action are:

$$G_{\mu\nu} = \frac{8\pi}{\phi} c^4 T_{\mu\nu} + \frac{\omega}{\phi^2} \left[\partial_\mu \phi \partial_\nu \phi - \frac{1}{2} g_{\mu\nu} \partial_\alpha \phi \partial^\alpha \phi \right] + \frac{1}{\phi} \left[\nabla_\mu \nabla_\nu \phi - g_{\mu\nu} \square \phi \right]$$

$$\square \phi = \frac{8\pi T}{(3 + 2\omega)} c^4$$

Where:

- $G_{\mu\nu}$ is the Einstein tensor
- $T_{\mu\nu}$ is the energy-momentum tensor
- T is the trace of $T_{\mu\nu}$
- \square is the d'Alembertian operator

B. Key Predictions and Implications

The Brans-Dicke theory leads to several predictions that differ from those of General Relativity:

- Time-varying gravitational constant: The effective gravitational constant $G_{eff} = 1/\phi$ can vary with time and location.
- Modified cosmological evolution: The Friedmann equations are modified, potentially affecting the expansion history of the universe.
- Altered gravitational wave propagation: The theory predicts additional polarization modes for gravitational waves.
- Modified solar system dynamics: The theory predicts deviations from General Relativity in solar system tests, such as the precession of Mercury's orbit and light deflection by the Sun.

C. Observational Tests and Constraints

Various observations have been used to test and constrain the Brans-Dicke theory:

1. Solar System tests: Measurements of the Shapiro time delay by the Cassini spacecraft have placed tight constraints on the Brans-Dicke parameter $\omega > 40,000$ [4].
2. Cosmological observations: Big Bang Nucleosynthesis and Cosmic Microwave Background data have been used to constrain the variation of the gravitational constant [19].
3. Binary pulsar observations: The orbital decay of binary pulsars provides stringent tests of gravitational theories [20].

4. Gravitational wave observations: The detection of gravitational waves by LIGO/Virgo has placed new constraints on alternative theories of gravity [1].

Table 1: It summarizes some of the key observational constraints on the Brans-Dicke theory:

Observational Test	Constraint on ω
Cassini Shapiro delay	$\omega > 40,000$
Lunar Laser Ranging	$\omega > 1000$
Binary Pulsar PSR J1738+0333	$\omega > 25,000$

Despite these tight constraints, the Brans-Dicke theory remains an important conceptual framework for exploring alternatives to General Relativity and has inspired the development of more general scalar-tensor theories.

IV. Modified Newtonian Dynamics (MOND)

Modified Newtonian Dynamics (MOND) is an alternative theory of gravity proposed by Mordehai Milgrom in 1983 as a way to explain galactic rotation curves without the need for dark matter [12]. MOND modifies Newton's laws of motion at very low accelerations, typical of galactic scales.

A. Theoretical Foundation

The basic premise of MOND is that Newton's second law of motion, $F = ma$, is modified for very small accelerations. The modified law takes the form:

$$F = m \mu(a/a_0) a$$

Where:

- a_0 is a fundamental acceleration scale (approximately $1.2 \times 10^{-10} \text{ m/s}^2$)
- $\mu(x)$ is an interpolation function that transitions between the Newtonian and MONDian regimes

The function $\mu(x)$ has the following properties:

- $\mu(x) \approx 1$ for $x \gg 1$ (Newtonian regime)
- $\mu(x) \approx x$ for $x \ll 1$ (deep MOND regime)

One commonly used form for $\mu(x)$ is:

$$\mu(x) = x / (1 + x)$$

In the deep MOND regime, this leads to a modified gravitational force law:

$$F = \sqrt{GMa_0} / r$$

This results in flat rotation curves for galaxies without the need for dark matter.

B. Key Predictions and Implications

MOND makes several distinct predictions:

1. Flat rotation curves: Galaxies should exhibit flat rotation curves at large radii without the need for dark matter.
2. Tully-Fisher relation: MOND naturally predicts the observed Tully-Fisher relation between galaxy luminosity and rotation velocity.
3. External field effect: The dynamics of a system can be affected by external gravitational fields, even in the absence of tidal forces.
4. Gravitational lensing: MOND predicts different lensing effects compared to General Relativity with dark matter.
5. Galaxy cluster dynamics: MOND faces challenges in explaining the dynamics of galaxy clusters without additional dark matter.

C. Observational Tests and Challenges

MOND has been successful in explaining several observed phenomena:

1. Galactic rotation curves: MOND provides good fits to observed rotation curves of galaxies without the need for dark matter [18].
2. Tully-Fisher relation: The observed Tully-Fisher relation is a natural consequence of MOND [11].
3. Dwarf galaxies: MOND explains the dynamics of dwarf galaxies, which are challenging for the standard cold dark matter model [9].

However, MOND also faces significant challenges:

1. Galaxy clusters: MOND requires additional dark matter to explain the dynamics and X-ray emissions of galaxy clusters [17].
2. Gravitational lensing: While MOND can explain some lensing observations, it struggles with others, particularly in galaxy clusters [6].
3. Cosmic Microwave Background: MOND, in its original form, does not provide a cosmological framework to explain the observed CMB anisotropies.
4. Bullet Cluster: Observations of colliding galaxy clusters, such as the Bullet Cluster, pose challenges for MOND [6].

V. Conformal Cyclic Cosmology

Conformal Cyclic Cosmology (CCC) is a cosmological model proposed by Roger Penrose in 2010 as an alternative to the standard inflationary Big Bang model [13]. CCC suggests that the universe undergoes endless cycles of expansion and contraction, with each cycle (or "aeon") beginning with a Big Bang and ending in a state similar to the remote future of our current aeon.

A. Theoretical Foundation

The key idea behind CCC is that the very early universe (immediately after the Big Bang) and the very late universe (in the remote future) are physically equivalent when considered in terms of conformal geometry. This equivalence allows for a smooth transition between aeons.

The main postulates of CCC are:

1. The universe will expand forever, approaching a state of extremely low matter density and dominated by massless particles (photons and gravitons).
2. In this low-density state, all particles become effectively massless, and the universe becomes scale-invariant (conformal).
3. The conformal structure of this late universe can be mapped onto the conformal structure of the very early universe of the next aeon.
4. This mapping provides a mechanism for the smooth transition between aeons, effectively "recycling" the universe.

B. Key Predictions and Implications

CCC makes several distinctive predictions:

1. Concentric circles in the CMB: CCC predicts the existence of concentric circles of low variance in the Cosmic Microwave Background, which would be signatures of gravitational waves from supermassive black hole collisions in the previous aeon.
2. No primordial gravitational waves: Unlike inflationary models, CCC does not predict primordial gravitational waves from the Big Bang.
3. Resolution of the entropy problem: CCC provides a potential solution to the problem of low initial entropy in the universe by relating it to the high entropy state at the end of the previous aeon.
4. Dark matter as gravitational wave remnants: CCC suggests that dark matter could be composed of gravitational wave remnants from the previous aeon.

C. Observational Tests and Challenges

Testing CCC is challenging due to the vast timescales involved and the difficulty in distinguishing its predictions from those of other models. However, some potential tests have been proposed:

1. CMB anomalies: Searches for concentric circles of low variance in the CMB have yielded mixed results, with some studies claiming evidence for such features and others finding no significant signal [2,10].
2. Gravitational wave background: Future gravitational wave detectors might be able to probe the gravitational wave background predicted by CCC.
3. Large-scale structure: The distribution of galaxies and galaxy clusters might contain imprints of structures from the previous aeon.

VI. Comparison Of Models

To provide a comprehensive overview of the alternative cosmological models discussed in this paper, we present a comparative analysis of their key features, strengths, and challenges. This comparison also includes the standard Lambda-CDM model as a reference point.

Table 2: Comparison of Cosmological Models

Feature	Lambda-CDM	Brans-Dicke	MOND	CCC
Gravity Theory	General Relativity	Scalar-Tensor	Modified Newtonian	Conformal Gravity
Dark Matter	Required	Required	Not Required	Potentially Explained
Dark Energy	Cosmological Constant	Scalar Field	Not Addressed	Not Required
Inflation	Separate Theory Required	Potentially Explained	Not Addressed	Not Required
CMB Predictions	Accurate	Similar to Lambda-CDM	Challenges	Unique Features
Galactic Dynamics	Requires Dark Matter	Similar to Lambda-CDM	Naturally Explained	Not Directly Addressed
Gravitational Waves	Consistent	Additional Modes	Challenges	Unique Predictions
Observational Support	Strong	Constrained	Mixed	Limited

Each of these models has its strengths and weaknesses:

1. Lambda-CDM:

- Strengths: Excellent fit to a wide range of observational data, including CMB, large-scale structure, and Type Ia supernovae.
- Weaknesses: Requires unexplained dark matter and dark energy components, faces small-scale challenges (e.g., core-cusp problem).

2. Brans-Dicke Theory:

- Strengths: Incorporates Mach's principle, potential for addressing inflation.
- Weaknesses: Highly constrained by solar system tests, requires fine-tuning to match Lambda-CDM predictions.

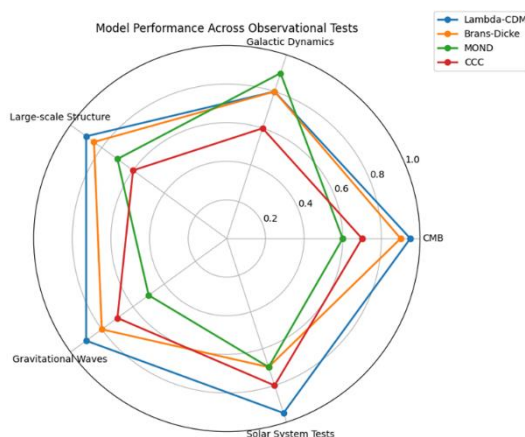
3. MOND:

- Strengths: Naturally explains galactic rotation curves and the Tully-Fisher relation without dark matter.
- Weaknesses: Struggles with galaxy cluster dynamics and cosmological observations, lacks a fully covariant formulation.

4. Conformal Cyclic Cosmology:

- Strengths: Addresses the low initial entropy problem, provides an alternative to inflation.
- Weaknesses: Limited observational evidence, challenges in explaining structure formation.

To visualize the relative performance of these models across different observational tests, we present a radar chart:



This radar chart provides a visual representation of how well each model performs across different observational tests. The scores are qualitative assessments based on the current state of research and are intended to illustrate the relative strengths and weaknesses of each model.

VII. Conclusion And Future Scope

This paper has explored three alternative cosmological models that diverge from the traditional Einstein-de Sitter framework: the Brans-Dicke theory, Modified Newtonian Dynamics (MOND), and Conformal Cyclic Cosmology (CCC). Each of these models offers unique perspectives on the nature of gravity, the evolution of the universe, and potential solutions to current cosmological challenges.

The Brans-Dicke theory, with its incorporation of Mach's principle and a variable gravitational constant, provides an intriguing framework for exploring modifications to General Relativity. However, tight observational constraints have limited its viability as a complete alternative to the standard model.

MOND has been remarkably successful in explaining galactic dynamics without the need for dark matter, but it faces significant challenges in addressing cosmological observations and lacks a fully covariant formulation. Ongoing research into relativistic extensions of MOND, such as TeVeS (Tensor-Vector-Scalar gravity), may help address some of these issues [3].

Conformal Cyclic Cosmology offers a radical reimagining of the universe's evolution, potentially resolving the problem of initial low entropy and providing an alternative to cosmic inflation. However, it remains highly speculative and requires further observational support.

While none of these alternative models currently rival the observational success of the Lambda-CDM model, they play a crucial role in cosmological research by:

1. Challenging assumptions: These models encourage critical examination of the foundations of our cosmological theories.
2. Inspiring new ideas: Concepts from alternative models often find applications in mainstream cosmology or lead to new hybrid theories.
3. Driving observational progress: The unique predictions of these models motivate new observational tests and improve our understanding of the universe.

Future research directions in this field should focus on:

1. Developing more comprehensive theoretical frameworks that can address multiple cosmological challenges simultaneously.
2. Improving observational tests to distinguish between competing models, particularly at scales where predictions diverge.
3. Exploring connections between alternative cosmological models and other areas of physics, such as particle physics and quantum gravity.
4. Investigating hybrid models that incorporate elements from multiple theories to address the strengths and weaknesses of individual approaches.
5. Utilizing advanced computational techniques and machine learning to analyze complex cosmological datasets and test model predictions.

In conclusion, while the Lambda-CDM model remains the most successful description of our universe, the exploration of alternative cosmological models continues to be a vital and dynamic area of research. These models not only challenge our understanding but also inspire new ways of thinking about the cosmos, driving progress in both theoretical and observational cosmology. As we gather more precise observational data and develop more sophisticated theoretical tools, we may yet uncover new insights that revolutionize our understanding of the universe.

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