

Restriction of Soft Sets and Soft Mappings and Some of its Real Life Applications

Majd Hamid Mahmood

Department of Mathematics Collage of Education,
Al-Mustansiriyah University, Baghdad, Iraq .

Abstract

In this search we define the restriction of soft set in two methods ,first method ,the restriction of soft set (F,E) on $A \subset E$ (E is the set of parameters),second method ,the restriction of soft set (F,E) with respect to $A \subset X$ (X is the universal set) , introduce some practical examples .Then ,we introduce and study restriction of soft mappings .

Key words : restricted soft set, soft topology ,image processing , restriction of soft mappings .

Date of Submission: 18-07-2020

Date of Acceptance: 03-08-2020

I. INTRODUCTION

soft set was introduced in [8] by Molodtsov. Maji and Roy [7] introduced operations on soft sets, new operations in soft set was introduced in [2],[5] by Irfan and Feng, in [1],[3],[4] , [10] properties of soft topological spaces has been studied , [9],[6] introduce a new studies on soft spaces ,soft relative topology is defined in [3], soft mapping defined in [11] by Wardowski .

In this search we will define the restriction of soft set, give an examples in restriction of a matrix of pixels . Then, introduce the restriction mappings over a soft set , study the restriction of mapping on soft continuous , soft open, soft close maps , we would like to mention that all soft sets in this search are on the same set of parameters E , denoted by $S(X)_E$,through this search simply (A,E) equals to \tilde{A} , (F,E) equals to \tilde{F} .

Definition 1.1.[5][7]

- 1- The soft set (F,E) over X is said to be a (null soft set) denoted by $\tilde{\Phi}$, if $\forall e \in E, F(e) = \Phi$, (Φ the null set) .
- 2- The soft set (F,E) over X is said to be an (absolute soft set) denoted by \tilde{X} if $\forall e \in E, F(e) = X$.
- 3- Let (F,A) , (G,B) be two soft sets in $S(X)_E$, we say that (F,A) is a soft subset of (G,B) denoted $(F,A) \subseteq (G,B)$ if (i) $A \subseteq B$ and (ii) $F(e) \subseteq G(e) \forall e \in A$.
- 4- The soft difference (H,E) of two soft sets (F,E) and (G,E) over X denoted by $(F,E) \setminus (G,E)$ is defined as $H(e) = F(e) \setminus G(e)$ for all $e \in E$.
- 5- The union of two soft sets of (F,A) and (G,B) over the common universe X is the soft set (H,C) , where $C = A \cup B$, and $\forall e \in C$ we write $(F,A) \cup (G,B) = (H,C)$,

$$H(e) = \begin{cases} F(e) & \text{if } e \in A \setminus B \\ G(e) & \text{if } e \in B \setminus A \\ F(e) \cup G(e) & \text{if } e \in A \cap B \end{cases}$$

- 6- The intersection of two soft sets (F,A) and (G,B) over a common universe set X is the soft set (H,C) where $C = A \cap B$ and $\forall e \in C, H(e) = F(e) \cap G(e)$,we write $(F,A) \cap (G,B) = (H,C)$.

Definition 1.2. [10]

Let \tilde{T} be the collection of soft sets over X then \tilde{T} is soft topology on X if :

- 1- Φ, X belong to \tilde{T} .
 - 2- The union of any number of soft sets in \tilde{T} belongs to \tilde{T} .
 - 3- The intersection of any two soft sets in \tilde{T} belongs to \tilde{T} .
- The triple (X, \tilde{T}, E) is called a soft topological space over X .

II. The restriction of soft set on $A \subset E$ (E is the set of parameters)

Definition 2.1.

Let X the universal set , (F,E) is soft set where $F:E \rightarrow P(X)$ the restriction of (F,E) with respect to the set of parameters $A \subset E$ is (G,A) where $G:E \setminus A \rightarrow P(X)$, $F(e) = G(e) \quad \forall e \in A$.

Example 2.2.

Let $X = \{\text{Mathematics , Physics , Geology}\}$ represent the scientific information's that each book b_1 , b_2 and b_3 consist , E the set of parameters represent the set of three books = $\{ b_1 , b_2 , b_3 \}$, the soft set (F,E) represent the scientific information's that each book consist $(F,E) = \{ (b_1, \{\text{Mathematics}\}) , (b_2, \{\text{Mathematics , Physics}\}) , (b_3, \{X\}) \}$ Means that the book1 contains Mathematics only , b_2 contains Mathematics and physics , b_3 contains all Mathematics , Physics and Geology.

Let $A = \{ b_1 , b_2 \} \subset E$, $G:E \setminus A \rightarrow P(X)$. Then, $(G,A) = \{ (b_1, \{\text{Mathematics}\}) , (b_2, \{\text{Mathematics , Physics}\}) \}$ is the restriction of (F,E) with respect to A which represent only two books b_1 , b_2 .

Application 2.3.

A Pixel is a sets of three numbers that together to represent a particular color.

In this example we will restrict an image on 3×3 matrix of Pixels by using the concept " restriction of soft sets "

Let X represent the three colors read , green and blue the degree of each color n equals 0 to 255,

$X = \{R_n, G_n, B_n\}$ for some n , E the set of parameters represent the set of n -Pixels

$E = \{p_{ij}, i = j = \{1,2,3\}\}$, the soft set (F,E) represent the image that contain 9 Pixels

$(F,E) = \{ (p_{11}, \{R_{255}, G_0, B_0\}) , (p_{21}, \{R_{102}, G_{102}, B_{255}\}) , (p_{31}, \{R_{51}, G_{204}, B_{153}\}) , (p_{12}, \{R_{255}, G_{255}, B_{102}\}) , (p_{22}, \{R_{255}, G_0, B_{204}\}) , (p_{32}, \{R_{51}, G_{204}, B_{255}\}) , (p_{13}, \{R_{51}, G_{51}, B_0\}) , (p_{23}, \{R_{51}, G_{51}, B_{153}\}) , (p_{33}, \{R_{255}, G_{153}, B_{153}\}) \}$.

Let $A = \{ p_{11}, p_{21}, p_{12}, p_{22} \} \subset E$, $C: E \setminus A \rightarrow P(X)$.

Then, $(C,A) = \{ (p_{11}, \{R_{255}, G_0, B_0\}) , (p_{21}, \{R_{102}, G_{102}, B_{255}\}) , (p_{12}, \{R_{255}, G_{255}, B_{102}\}) , (p_{22}, \{R_{255}, G_0, B_{204}\}) \}$ is the restriction of (F,E) with respect to A .



Figure 1. This figure show the restriction of 3×3 matrix of Pixels in to a of 2×2 matrix of Pixels .

Application 2.4.

Let X represent the three colors read , green and blue the degree of each color n equals 0 to 255,

$X = \{R_n, G_n, B_n\}$ for some n ,

E the set of parameters represent the set of n -Pixels

$E = \{p_{ij}, i = j = \{1,2,3\}\}$, the soft set (F,E) represent the image that contain 9 Pixels

$(F,E) = \{ (p_{11}, \{R_{255}, G_0, B_0\}) , (p_{21}, \{R_{102}, G_{102}, B_{255}\}) , (p_{31}, \{R_{51}, G_{204}, B_{153}\}) , (p_{12}, \{R_{255}, G_{255}, B_{102}\}) , (p_{22}, \{R_{255}, G_0, B_{204}\}) , (p_{32}, \{R_{51}, G_{204}, B_{255}\}) , (p_{13}, \{R_{51}, G_{51}, B_0\}) , (p_{23}, \{R_{51}, G_{51}, B_{153}\}) , (p_{33}, \{R_{255}, G_{153}, B_{153}\}) \}$.

Let $B = \{ p_{21}, p_{22}, p_{23}, p_{31}, p_{32}, p_{33} \} \subset E$, $C: E \setminus B \rightarrow P(X)$.

Then, $(C,B) = \{ (p_{11}, \{R_{255}, G_{255}, B_{102}\}) , (p_{31}, \{R_{51}, G_{51}, B_0\}) , (p_{22}, \{R_{255}, G_0, B_{204}\}) , (p_{23}, \{R_{51}, G_{204}, B_{255}\}) , (p_{32}, \{R_{51}, G_{51}, B_{153}\}) , (p_{33}, \{R_{255}, G_{153}, B_{153}\}) \}$ is the restriction of (F,E) with respect to B .



Figure 2. This figure show the restriction of 3×3 matrix of Pixels in to a of 2×3 matrix of Pixels .

Propositions2.5.

Let X be the universal set, for a given soft set the restricted soft set (with respect to $A \subset E$) is a special case of soft subset .

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,A) is the restriction of (F,E) with respect to the set of parameters $A \subset E$ where $G:E \setminus A \rightarrow P(X)$, since (i) $A \subseteq E$ and (ii) $G(e) \subseteq F(e) \forall e \in A$.Then, $(G,A) \subseteq (F,E)$.

Propositions2.6.

Let X be the universal set , the soft union of a soft set with restricted soft set (with respect to $A \subset E$) is a soft set.

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,A) is the restriction of (F,E) with respect to the set of parameters $A \subset E$ where $G:E \setminus A \rightarrow P(X)$, since $e \in A \cap E$ and $F(e) \cup G(e) = F(e)$.Then, $(F,E) \cup (G,A) = (F,E)$.

Propositions2.7.

Let X be the universal set, the soft intersection of soft set with the restricted soft set (with respect to $A \subset E$) is the restricted soft set .

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,A) is the restriction of (F,E) with respect to the set of parameters $A \subset E$ where $G:E \setminus A \rightarrow P(X)$, since $F(e) = G(e) \forall e \in A$.Then, $(F,E) \cap (G,A) = (G,A)$.

III. The restriction of soft set with respect to $A \subset X$ (X is the universal set)

Definition 3.1. Let X be a universal set let (F,E) be a soft set where $F:E \rightarrow P(X)$ the restriction of soft set (F,E) with respect to a subset A of a universal set X is a soft set (G,E) where $G : E \rightarrow F(e) \cap A , \forall F(e) \in p(X)$ where $G(e) = F(e) \cap A , \forall e \in E$.

Example 3.2. Let $X = \{a, b, c\}$ be a set of three fonts, E the set of parameters represent the set of three words $= \{ w_1, w_2, w_3 \}$ where $(F,E) = \{ (w_1, \{ a, b, c \}) , (w_2, \{ a, c, b \}) , (w_3, \{ \Phi, \Phi, \Phi \}) \}$ (F,E) is a statement contain three words with fonts a, b, c arranged in different ways . so $(G,E) = \{ (w_1, \{ a, b, c \}) , (w_2, \{ a, \Phi, \Phi \}) , (w_3, \{ \Phi, \Phi, \Phi \}) \}$ is a restricted soft set with respect to A .

Application 3.3. Let $X = \{ x, y, z \}$, x, y, z are arbitrary three numbers belongs to the set of natural numbers, X represent the set of point in three dimension ,

E the set of parameters represent the set of three points in time $= \{ t_1, t_2, t_3 \}$

$(F,E) = \{ (t_1, \{ x_1, y_1, z_1 \}) , (t_2, \{ x_2, y_2, z_2 \}) , (t_3, \{ x_3, y_3, z_3 \}) \}$

represent a particle in a specific three dimension space moves through a specific three points in time ,

$\tilde{\Phi} = \{ (t_1, \{ 0,0,0 \}) , (t_2, \{ 0,0,0 \}) , (t_3, \{ 0,0,0 \}) \}$ represents a particle in a three dimension space does not exist in the three discrete points of time,

$\tilde{X} = \{ (t_1, X) , (t_2, X) , (t_3, X) \}$ represent a particle in a three dimension space exist at three discrete points of

time, $\tilde{T} = \{ \tilde{\Phi}, \tilde{X}, (F,E) \}$ represent several probabilities of a particle in three dimension through three points in

time .Let $A = \{ x_7, y_7, 0 \} \subset X$, for a special case (for numbers we replace the intersection with minimum) where $x_4 = \min \{ x_1, x_7 \}$, $y_4 = \min \{ y_1, y_7 \}$,

$$z_4 = \min \{ z_1, 0 \} = 0, x_5 = \min \{ x_2, x_7 \}, y_5 = \min \{ y_2, y_7 \}, z_5 = \min \{ z_2, 0 \} = 0$$

$$x_6 = \min \{ x_3, x_7 \}, y_6 = \min \{ y_3, y_7 \}, z_6 = \min \{ z_3, 0 \} = 0.$$

Then $(G,E) = \{ (t_1, \{ x_4, y_4, 0 \}), (t_2, \{ x_5, y_5, 0 \}), (t_3, \{ x_6, y_6, 0 \}) \}$ which is a particle in two dimension moves through the same three points in time t_1, t_2, t_3 .

Propositions 3.4.

Let X be the universal set, for a given soft set the restricted soft set (with respect to $A \subset X$) is a special case of soft subset.

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,E) is the restriction of (F,E) with respect to $A \subset X$ where $G : E \rightarrow F(e) \cap A, \forall F(e) \in P(X)$, since (i) $E \subseteq E$ and (ii) $G(e) \subseteq F(e) \forall e \in A$. Then, $(G,A) \subseteq (F,E)$.

Propositions 3.5.

Let X be the universal set, the soft union of a soft set with restricted soft set (with respect to $A \subset X$) is a soft set.

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,E) is the restriction of (F,E) with respect to $A \subset X$ where $G : E \rightarrow F(e) \cap A, \forall F(e) \in P(X)$, since $e \in E \cap E$ and $F(e) \cup G(e) = F(e)$. Then, $(F,E) \cup (G,E) = (F,E)$.

Propositions 3.6.

Let X be the universal set, the soft intersection of soft set with the restricted soft set (with respect to $A \subset X$) is the restricted soft set.

Proof :

Let (F,E) is soft set where $F:E \rightarrow P(X)$, (G,E) is the restriction of (F,E) with respect to $A \subset X$ where $G : E \rightarrow F(e) \cap A, \forall F(e) \in P(X)$, since $G(e) = F(e) \cap A = F(e) \forall e \in A$ then $(G,E) \cap (F,E) = (G,E), \forall e \in E$.

IV. Restriction of soft mappings

Definition 4.1. [11]

Let $(F,E), (G,E)$ are soft sets in $S(X)_E$. A soft relation $\tilde{f} \subseteq (F,E) \times (G,E)$ is called a soft mapping from (F,E) to (G,E) [denoted by $\tilde{f} : (F,E) \Rightarrow (G,E)$] if the following two conditions are satisfied :

- (i) for each soft element $\tilde{x} \in (F,E)$, there exists only one soft element $\tilde{y} \in (G,E)$ such that $\tilde{x} \tilde{f} \tilde{y}$ which will be noted as $\tilde{f}(\tilde{x}) = \tilde{y}$,
- (ii) for each empty soft element $\tilde{x} \in (F,E)$, $\tilde{f}(\tilde{x})$ is an empty soft element of (G,E) .

Definition 4.2.[3]

Let (X, \tilde{T}, E) be a soft topological space over X , (F, E) be a non-empty soft subset of (X, \tilde{T}, E) . Then, $\tilde{T}_F = \{ (F, E)^* = (F, E) \cap (G, E), \forall (G, E) \in \tilde{T} \}$ is the soft relative topology on (F, E) and $((F, E), \tilde{T}_F, E)$ is called soft subspace topology of (X, \tilde{T}, E) .

Definition 4.3.[3]

Let $\tilde{f} : (X, \tilde{T}_X, E) \Rightarrow (Y, \tilde{T}_Y, E)$ be a soft mapping between two soft topological spaces if the image $\tilde{f}((F, E))$ of each soft open set (soft close set) (F, E) over X is a soft open set (soft close set) in Y . Then, \tilde{f} is said to be a soft open mapping (soft close mapping).

Theorem 4.4.

The restriction of soft open (soft close) map over a soft open (soft close) set is soft open (soft close) map.

Proof

Let $\tilde{f} : (X, \tilde{T}_X, E) \Rightarrow (Y, \tilde{T}_Y, E)$ be a soft open mapping between two soft topological spaces, (A, E) be a soft open set in (X, \tilde{T}_X, E) to prove $\tilde{f}(A, E) : ((A, E), \tilde{T}_A, E) \Rightarrow (Y, \tilde{T}_Y, E)$ is soft open map, (G, E) be a soft open subset in (A, E) then $(G, E) \cap (A, E) = (G, E)$ is soft open set in \tilde{T}_X by soft relative topology definition, since \tilde{f} is soft open map then $\tilde{f}((G, E))$ is soft open in \tilde{T}_Y so prove $\tilde{f} | ((A, E), \tilde{T}_A, E)$ is soft open map, similarly for close case.

Example 4.5.

Let $X = \{h_1, h_2\}$, $Y = \{k_1, k_2\}$, $E = \{e_1, e_2\}$, the soft map $\tilde{f} : (X, \tilde{T}_d, E) \Rightarrow (Y, \tilde{T}_d, E)$ defined as follow :
 $\tilde{f}((e_i, \{h_j\})) = ((e_i, \{k_j\}))$, $\forall i, j = 1, 2$ is soft open and soft closed map .

Definition 4. 6.[11]

$\tilde{f} : (X, \tilde{T}_x, E) \Rightarrow (Y, \tilde{T}_y, E)$ is a soft continuous mapping if for each soft open set (G, E) over Y , $\tilde{f}^{-1}((G, E))$ is a soft open set over X .

Theorem 4.7.

The restriction of soft continuous mapping over a soft open set (soft close set) is soft continuous .

Proof : Let $\tilde{f} : (X, \tilde{T}_x, E) \Rightarrow (Y, \tilde{T}_y, E)$ be a soft continuous mapping between two soft topological spaces , (A, E) be a soft open set in (X, \tilde{T}_x, E) , the restriction of \tilde{f} on (A, E) is the mapping

$\tilde{f}|((A, E), \tilde{T}_A, E) : ((A, E), \tilde{T}_A, E) \Rightarrow (Y, \tilde{T}_y, E)$, to prove

$\tilde{f}|((A, E), \tilde{T}_A, E)$ is soft continuous map , (G, E) be a soft open set in \tilde{T}_y .

Then, $(\tilde{f}|((A, E), \tilde{T}_A, E))^{-1}((G, E)) = \tilde{f}^{-1}((G, E)) \cap (A, E)$

since \tilde{f} is soft continuous then $\tilde{f}^{-1}((G, E))$ is soft open set in \tilde{T}_x

by soft relative topology definition $\tilde{f}^{-1}((G, E)) \cap (A, E)$ is soft open in \tilde{T}_A ,

so $\tilde{f}|((A, E), \tilde{T}_A, E)$ is soft continuous map, similarly for close case .

Example 4. 8.

Let $X = \{h_1, h_2, h_3\}$, $E = \{e_1, e_2\}$ and

$\tilde{T} = \{\tilde{\Phi}, \tilde{X}, \{(e_1, \{h_2\}), (e_2, \{h_1\})\}, \{(e_1, \{h_1, h_3\}), (e_2, \{h_2, h_3\})\}, \{(e_1, \{h_2\}), (e_2, X)\}, \{(e_1, \Phi), (e_2, \{h_1\})\}, \{(e_1, \{h_1, h_3\}), (e_2, X)\}, \{(e_1, \Phi), (e_2, \{h_2, h_3\})\}, \{(e_1, \Phi), (e_2, X)\}$ and

$\tilde{T}' = \{\tilde{\Phi}, \tilde{X}, (e_1, \{h_2\}), (e_2, \{h_1\}), \{(e_1, \{h_2, h_3\}), (e_2, \{h_1, h_2\})\}, \{(e_1, \{h_1, h_2\}), (e_2, X)\}, \{(e_1, \{h_2\}), (e_2, \{h_1, h_2\})\}$,

let $\tilde{f} : (X, \tilde{T}, E) \Rightarrow (X, \tilde{T}', E)$ be a mapping defined as

$\tilde{f}((e_i, h_j)) = (e_i, h_i)$, $i = 1, 2$, $j = 1, 2, 3$. Then, \tilde{f} is a soft continuous .

Let $\tilde{A} = \{(e_1, \Phi), (e_2, \{h_1\})\}$ be a soft subset of \tilde{T} .

Then, $\tilde{T}_A = \{\{(e_1, \Phi), (e_2, \Phi)\}, \{(e_1, \Phi), (e_2, \{h_1\})\}\} = \{\tilde{\Phi}_A, \tilde{A}\}$

$\tilde{g}(\tilde{x}) = \tilde{f}(\tilde{x}) \forall \tilde{x} \in ((A, E), \tilde{T}_A, E)$.

Then, $\tilde{g} = \tilde{f}|((A, E), \tilde{T}_A, E) : ((A, E), \tilde{T}_A, E) \Rightarrow (X, \tilde{T}', E)$ is soft continuous map since

$\tilde{g}^{-1}(\tilde{\Phi}_A) = \tilde{\Phi}_A \in \tilde{T}_A$,

$\tilde{g}^{-1}(\tilde{X}) = \tilde{g}^{-1}(\{(e_1, X), (e_2, X)\}) = \{(e_1, X), (e_2, X)\} \cap \tilde{A} = \tilde{A} \in \tilde{T}_A$

$\tilde{g}^{-1}(\{(e_1, \{h_2\}), (e_2, \{h_1\})\}) = \{(e_1, \Phi), (e_2, X)\} \cap \tilde{A} = \tilde{A} \in \tilde{T}_A$

$\tilde{g}^{-1}(\{(e_1, \{h_2, h_3\}), (e_2, \{h_1, h_2\})\}) = \{(e_1, \Phi), (e_2, \{h_1\})\} \cap \tilde{A} = \tilde{A} \in \tilde{T}_A$

$\tilde{g}^{-1}(\{(e_1, \{h_1, h_2\}), (e_2, X)\}) = \{(e_1, \{h_1\}), (e_2, \{h_1\})\} \cap \tilde{A} = \tilde{A} \in \tilde{T}_A$

$\tilde{g}^{-1}(\{(e_1, \{h_2\}), (e_2, \{h_1, h_2\})\}) = \{(e_1, \Phi), (e_2, \{h_1\})\} \cap \tilde{A} = \tilde{A} \in \tilde{T}_A$

V. Conclusions

Any soft set (F, E) can be restricted in two ways :

First method - The restriction of soft set (F, E) on $A \subset E$ (E is the set of parameters) ,

as example we restricted a matrix of pixels which can be used in image processing in computer or printers .

Second method- The restriction of soft set (F, E) with respect to $A \subset X$ (X is the universal set)

as example suppose a soft set (F, E) represent a particle in a specific three dimension space moves through a

specific three points in time . Then, the restriction of (F, E) with respect to a set $A \subset X$ will give the soft set

(G, E) which is a particle in two dimension moves through the same three points in time t_1, t_2, t_3 .

For a soft map $\tilde{f} : (X, \tilde{T}_x, E) \Rightarrow (Y, \tilde{T}_y, E)$ and $[((A, E), \tilde{T}_A, E)]$ is subspace of (X, \tilde{T}_x, E) , the restriction of \tilde{f} with respect to (A, E) is the map :

$\tilde{g} = \tilde{f}|((A, E), \tilde{T}_A, E) : ((A, E), \tilde{T}_A, E) \Rightarrow (Y, \tilde{T}_y, E)$, we prove that the restriction of soft open map over a soft open set is soft open map , the restriction of soft close map over a soft close set is soft close map and the restriction of soft continuous mapping over a soft open set (or soft close set) is soft continuous .

References

- [1] Hussain S., Ahmad B., "Some properties of soft topological spaces" , Computers and Mathematics with Applications , Vol. 62 ,(2011) , pp. 4058–4067 .
<file:///C:/Users/Zian/Downloads/1-s2.0-S0898122111008297-main.pdf>
- [2] Irfan Ali M., Feng F. , Liu X. , Min W.K., Shabir M." On some new operations in soft set theory , Computers and Mathematics with Applications " , Vol. 57 ,(2009), pp.1547–1553.
<https://dl.acm.org/doi/10.1016/j.camwa.2008.11.009>
- [3] Mahmood M.H. , "On Soft Topological Spaces", LAP Lambert Academic Publishing ISBN-13 978-613-9-94966-3, (2018) .
<https://www.lap-publishing.com/catalog/details/store/gb/book/978-613-9-94966-3/on-soft-topological-spaces>
- [4] Maji P.K.,Biswas R., Roy A. R., "Soft set theory", Computers and Mathematics with Applications, Vol.45, (2003) , pp.555-562 .
<https://reader.elsevier.com/reader/sd/pii/S0898122103000166?token=C26B6C38AC667EB1B38F83FEF424E00526F8481E97205AE55191E3B4BE6286AC5F9B512D943FC3375C08ADC8AC9048E3>
- [5] Molodtsov D., "Soft set theory – first results", Computers and Mathematics with Applications, Vol. 37, (1999), pp.19-31 .
<https://core.ac.uk/download/pdf/82496757.pdf>
- [6] Noori S.,Yousif Y.Y. , "Soft Simply Compact Spaces" Iraqi Journal of Science, Special Issue, (2020), pp.108-113.
<http://scbaghdad.edu.iq/eijs/index.php/eijs/article/view/2050>
- [7] OzturkT.Y.andKarademir M. , "Soft pair-wise b-continuity on soft bitopologicalspaces",AIP Conference Proceedings · April (2017) ,DOI: 10.1063/1.4981703 .
https://www.researchgate.net/publication/316486289_Soft_pair-wise_b-continuity_on_soft_bitopological_spaces
- [8] Peyghan E. , B.Samadi , A.Tayebi, " About soft topological spaces " , Journal of New Results in Science, No.2, (2013) ,pp. 60-75
https://www.researchgate.net/publication/266475237_About_soft_topological_spaces
- [9] Saif Z. Hameed*, Adiya K. Hussein , " On Soft bc-Open Sets in Soft Topological Spaces" , Iraqi Journal of Science, (2020), Special Issue, pp. 238-242.
<http://scbaghdad.edu.iq/eijs/index.php/eijs/article/view/2282>
- [10] Shabir M. , NazM., "On soft topological spaces" ,Computers and Mathematics with Applications ,Vol. 61 ,(2011), pp. 1786–1799 .
https://people.sc.fsu.edu/~jburkardt/classes/sc_2015/plagiarism/shabir.pdf
- [11] Wardowski D., "On a soft mapping and its fixed points", Springer Open Journal ,Vol. 182 , (2013), pp.1-11 .
<https://core.ac.uk/download/pdf/81814459.pdf>

Majd Hamid Mahmood. "Restriction of Soft Sets and Soft Mappings and Some of its Real Life Applications." *IOSR Journal of Mathematics (IOSR-JM)*, 16(4), (2020): pp. 33-38.