

## The Constants of Density-Velocity Relation for Density Estimation in Tau Field, Niger Delta Basin

\*Atat, J. G., \*\*Uko, E. D., \*\*Tamunobereton-ari, I. and \*\*\*Eze, C. L.

\*Department of Physics, University of Uyo, Nigeria

\*\*Department of Physics, Rivers State University, Port Harcourt, Nigeria

\*\*\*Institute of Geosciences and Space Technology, Rivers State University, Nigeria

Corresponding Author: Atat, J. G.

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**Abstract:** Well-log data covering three wells (AA, BB and CC) in Tau( $\tau$ ) Field in the Niger Delta were used for density-velocity constants evaluation. Using Hampson Russell Software, Gardner's and Lindseth's relations were localized and subsequently transformed to obtain the local fits constants:  $b$ ,  $n$ ,  $e$  and  $f$  for sand and shale lithologies. The correlation result of  $V_p$  with  $V_s$  is 0.93 which is a strong linear relationship; therefore, density can also be predicted using shear wave velocity data. The major findings resulting from the local fit for sands and shales differentiated, indicate  $b$  and  $n$  from compressional wave velocity as 0.23 and 0.27 (from shear wave velocity as 0.12 and 0.24) respectively for sand; 0.52 and 0.45 (from shear wave velocity as 0.23 and 0.30) respectively for shale. Also, the constants  $e$  and  $f$  from compressional wave velocity as 0.320 and 3481 (from shear wave velocity as 0.340 and 1640) respectively for sand; 0.35 and 1595 (from shear wave velocity as 0.35 and 8380) respectively for shale.

**Keywords:** Density, Velocity, Constants, Sand, Shale, Lithology and Well-Log Data.

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### I. Introduction

Density values overlap for sands and shales (with shales velocity lesser than that of sand). This makes density not a good lithological indicator. This property aids in identification of reservoir rock by lithology delineation; it is also useful in the detection of gas-bearing formations, the identification of evaporates and in ore content evaluation for mining activities (Kearey et al., 2002). It is used by Geoscientists and Reservoir Engineers to quantify and model reservoirs since it is a measure of reservoir quality in both clastic and carbonate rocks.

In order to obtain different density-velocity relations and their parameters, p-wave velocity, s-wave velocity, density and gamma ray data from a well can be used (Quijada & Stewart, 2007). Well-logs are used to determine velocity-density balances with Gardner-Lindseth connection aimed at valuing density.

Crossplotting density with rock properties, lithology and pore fluid indicate density as the property that gives the best differentiation between hydrocarbon reservoirs and other fluid types (Koughnet et al., 2003). This makes accurate density estimates significant for characterization of reservoir. By Gray et al. (2006), a proper estimate of density is required to determine the shale location which may prevent the steaming or recovery process.

### Location and Geology of the Study Area

$\tau$  Field is located 40 km southwest of Port Harcourt, Rivers State in the Niger Delta within latitudes  $3^{\circ}\text{N}$  and  $6^{\circ}\text{N}$ ; longitudes  $5^{\circ}\text{E}$  and  $8^{\circ}\text{E}$  (Figure 1). Niger Delta is characterized with two distinct seasons: Wet season (March till October) and dry season (November till February). The mean monthly rainfall during rainy season is about 135 mm and this falls to 65 mm during dry season (Atat, et al., 2012; George et al., 2010).

From the period of Eocene to the present, the delta has advanced towards the south, forming depobelts that stand for the most engaging portion of the delta at each stage of its development (Doust & Omatsola, 1990). These depobelts (Figure 1) form one of the deltas which is characterized by regression and it is the largest in the world with an area of  $300,000 \text{ km}^2$  (Kulke, 1995); sediment volume of  $500,000 \text{ km}^3$  (Hospers, 1965); sediment thickness of over 10 km in the basin depocenter (Kaplan et al., 1994). Niger Delta province contains only one identified petroleum system called the Tertiary Niger Delta (Akata-Agbada) petroleum system. The rock from primary source is the upper Akata formation. Oil is produced from sandstone facies within the Agbada formation; the main target is the turbidite sand located in the upper Akata formation in deep water offshore or may be onshore (Tuttle, et al., 1999; Kulke, 1995; Ekweozor & Daukoru, 1994). The formation has an estimate of up to  $7 \times 10^3$  metres thick (Doust & Omatsola, 1990). The Benin formation is about  $0.28 \times 10^3$  metres thick but

may be up to  $2.1 \times 10^3$  metres in the region of maximum subsidence (Whiteman, 1982), and consists of continental sands and gravels.



**Figure 1: Niger Delta Study Area with Base Map.**

Source: Kulke (1995)

### Theoretical Basis

The laws of Physics are applied to determine the distribution of reservoir fluids (gas, oil and water) trapped in a reservoir. Gardner et al., 1974 and Lindseth, 1979 have modelled density-velocity expressions for density estimate in their area of study. Their parameters could not give accurate prediction in the  $\tau$  Field or any other field in the Niger Delta basin since this basin was excluded in their study.

According to Gardner's relation:

$$\rho = aV_p^m \tag{1}$$

where  $a$  and  $m$  are Gardner's default parameters (constant coefficients);  $\rho$  is the bulk density;  $V_p$  is compressional wave velocity.

This relation is a good approximation for shales, sandstones and carbonates while coals and evaporates depart significantly from the expected behaviour (Gardner et al., 1974; Quijada and Stewart, 2007).

If equation 1 is localized to a parameter in our field of interest using  $b$  and  $n$  as constant coefficients for local fits. The expression becomes

$$\rho = bV_p^n \tag{2}$$

Taking the log of both sides of equation 2 and applying the laws of logarithm

$$\log \rho = \log b + n \log V_p \tag{3}$$

A plot of  $\log \rho$  versus  $\log V_p$  enables the deduction of  $b$  and  $n$  from the antilog of the intercept and the slope of the graph respectively.

From Lindseth's relation (or equation),

$$V_p = c\rho V_p + d \tag{4}$$

(Lindseth, 1979).

Considering it for the local fits constants for sand and shale, yields

$$V_p = e\rho V_p + f \tag{5}$$

$$\rho = \frac{V_p - f}{eV_p} \tag{6}$$

where  $e$  and  $f$  are local fit constants from least square fit approach;  $c$  and  $d$  are Lindseth's constants.

The use of special software (Hampson Russell) enables the crossplots that lead to achieving our purpose.

## II. Materials and Methods

### Materials

Hampson Russell Software was used for data loading, processing, crossplots and diagrams. Data acquired from the onshore Niger Delta oilfield are suites of Logs from three wells (Figures 2), markers, base map (Figures 1) and geology.

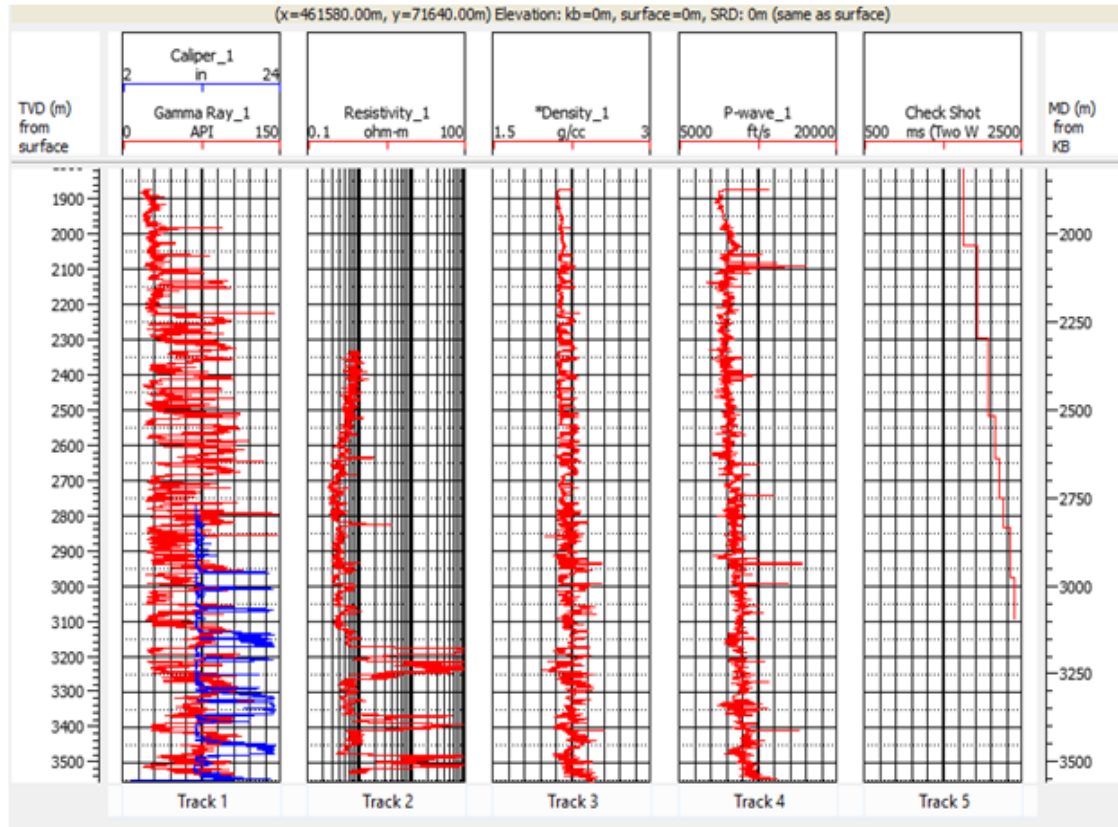


Figure 2.0: Suite of imported logs showing log signatures of Gamma ray, Resistivity, Density and P-wave velocity.

### Method

The log Import interface of the Hampson Russell Software (HRS) was used to import well data, tops applied, consistency of wellbore diameter checked with caliper log, the section of the log which was compromised edited out which results in figure 3 and other procedure stated in figure 4 lead to the estimation of these parameters.

Figure 4 breaks down the well-log analysis carried out to determine the reservoir zones, estimation of rock attribute (the s-wave velocity was generated from p-wave velocity information); performed crossplots analysis to estimate the parameters for local fits. A linear regression line that best fits the data in a least-squares sense was applied to these relationships to estimate the coefficients  $b$  and  $n$  from equation 3;  $e$  and  $f$  from equation 5 for sand and shale lithology.

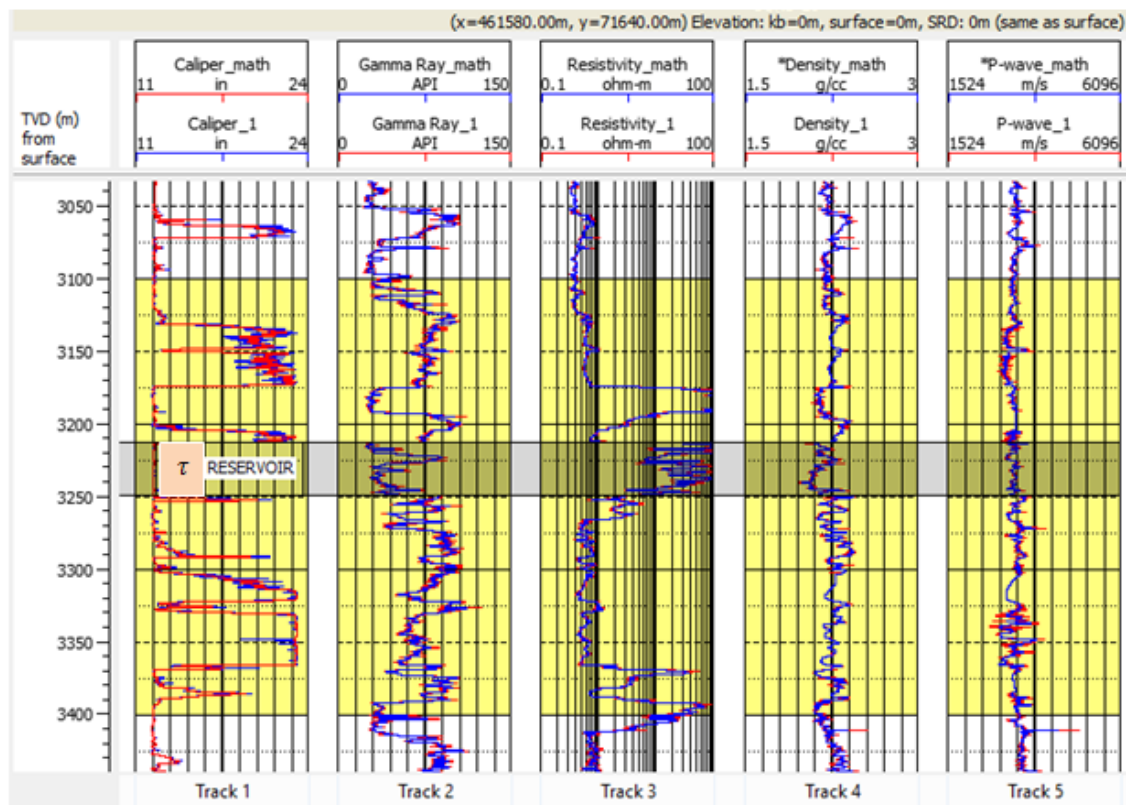


Figure 3: De-spiking of  $V_p$ ,  $\rho$  and other logs using log filtering utility of HRS (filtered logs in blue, unfiltered logs in red).

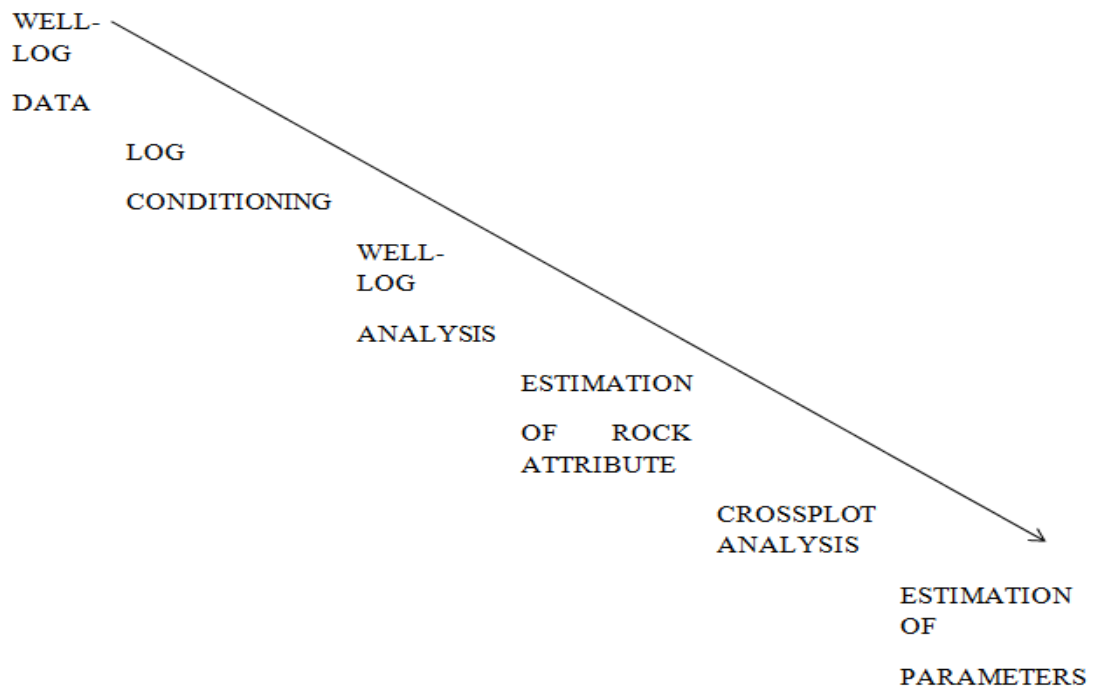


Figure 4: Workflow of Approach

### III. Results and Discussion

Three wells of  $\tau$  Field were analyzed to obtain constants for density-velocity relations; the results are presented in Figures 5 to 9 and Tables 1.

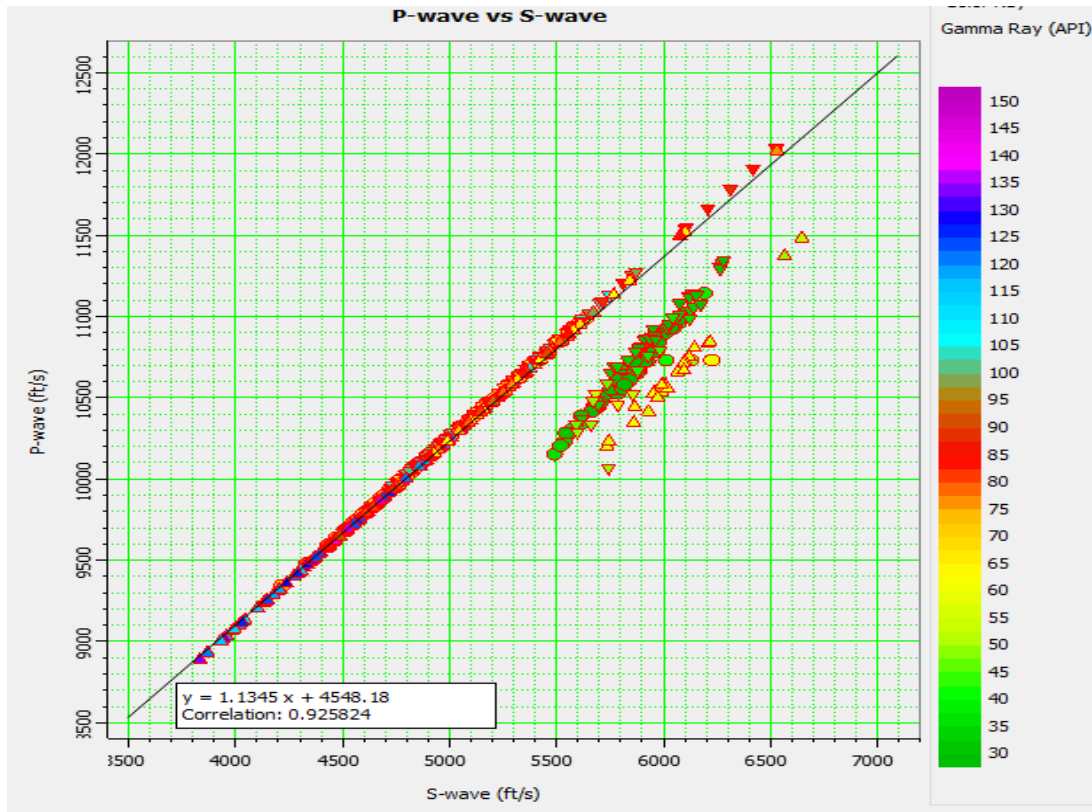


Figure 5: Correlation of  $V_p$  with  $V_s$  estimated using castagna's relation from the three wells

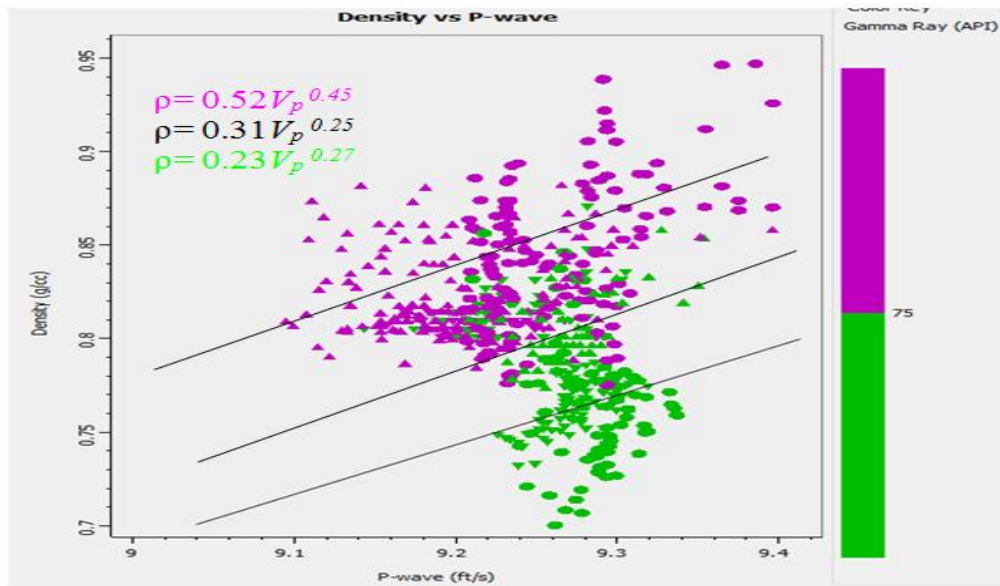


Figure 6: A plot of density versus  $V_p$  data for wells constants for sands (green) and shales (pink) with linear curve fitting using Gardner approach.

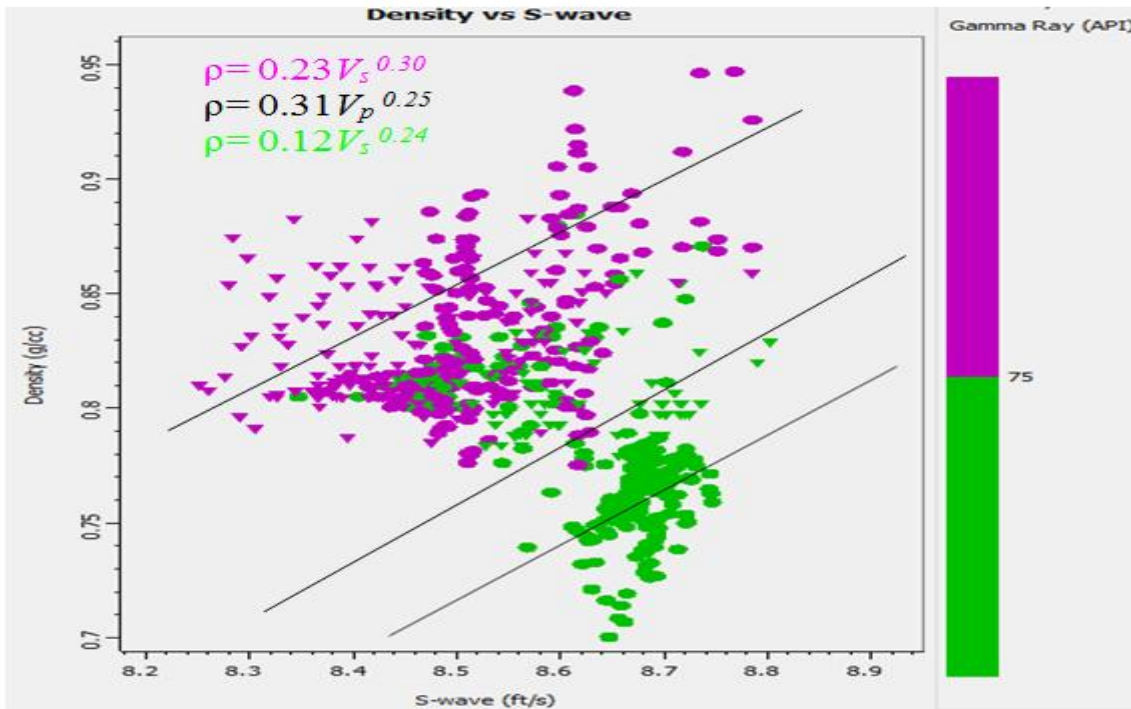


Figure 7: A plot of density versus  $V_s$  data for wells constants for sands (green) and shales (pink) with linear curve fitting using Gardner approach.

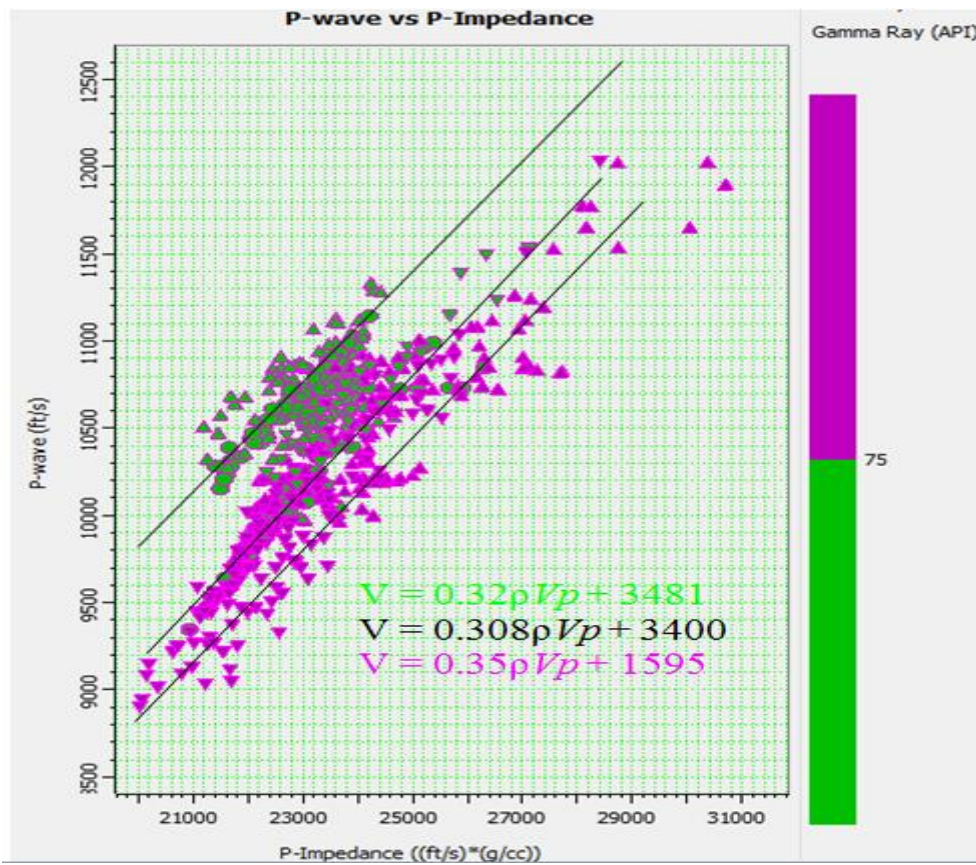


Figure 8: A plot of  $V_p$  versus p-impedance data for wells constants for sands (green) and shales (pink) with linear curve fitting using Lindseth approach

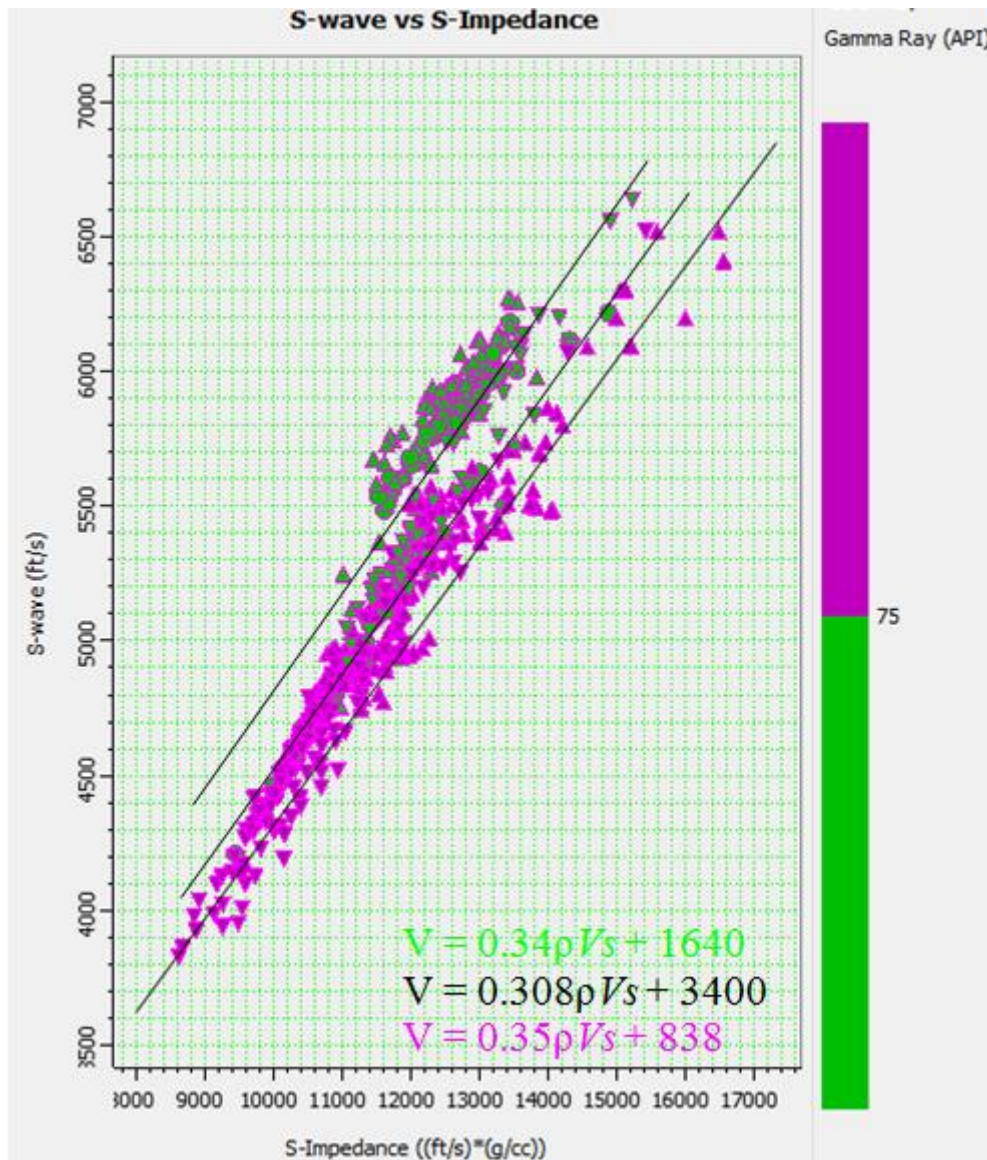


Figure 9: A plot of  $V_s$  versus s-impedance data for wells constants for sands (green) and shales (pink) with linear curve fitting using Lindseth approach.

Table 1: Estimated Constants (sands and shales) for Density Models.

Constants	Lithology			
	Sand from $V_p$	Sand from $V_s$	Shale from $V_p$	Shale from $V_s$
b	0.23	0.12	0.52	0.23
n	0.27	0.24	0.45	0.30
Gardner's default: b = 0.31 and n = 0.25				
e	0.320	0.340	0.350	0.350
f	3481	1640	1595	838
Lindseth default: e = 0.308 and f = 1054				

### Discussion

Shear wave velocity was achieved using Castagna's relation; the result was confirmed by investigating how strong-p-wave velocity relates with s-wave velocity as seen in figure 5. The correlation of 0.93 is very strong; the two parameters are linearly related.

The Gamma Ray (GR) as a lithology discriminator was used to aid the estimation of values of b and n for specific rock types by considering the graph of density versus velocities with samples in green having GR lower than 75 which is for sands; samples in magenta have GR higher than 75 which is for shales (figures 6 and 7). These two clusters are now clearly differentiated, though very little overlap still exists between the samples. The fit is significantly improved by using this separation, with less dispersion of points with respect to the fitted

line and coefficients closer to those defined by Gardner (This is from localized Gardner methodology). The new constants for local fits were obtained (Table 1).

The GR used to estimate values of  $e$  and  $f$  for specific rock types was with respect to the graph of velocities versus impedances with samples in green having GR lower than 75 which are for sands (Figures 8 and 9). The same cut-off of GR lower than 75 for sands (green); GR higher than 75 for shales (pink) with linear curve fitting using Lindseth approach was noted.

#### IV. Conclusion

Gardner's and Lindseth's relationships were employed and localized to obtain constants for specific rock types. Shear wave velocity  $V_s$  was generated from  $V_p$ ; correlated with each other to investigate their relation strength; the result shows, they are strongly related. Gardner and Lindseth developed their constants with only P-wave data; we have obtained the constants for sand and shale for  $\tau$  field using both P-wave and S-wave velocities from well-log data. This is different from their default parameters. Both researchers did not carry out their coefficients investigation for this field since it was not among their area of interest; as such do not give accurate constant for density estimation in the  $\tau$  field or any related field in the Niger Delta.

#### References

- [1]. Atat, J. G., Akpabio, G. T., George, N. J. & Umoren, E. B. (2012). Geophysical Assessment of Elastic Constants of Top Soil using Seismic Refraction Compressional Velocities in the Eastern Niger Delta. *International Journal of Modern Physics*, 1(1): 7 – 19.
- [2]. Doust, H. & Omatsola, E. (1990). Niger Delta. In: Edwards, J. D. & Santogrossi, P. A. Editions. *Divergent/Passive Margin Basins*. American Association of Petroleum Geologists Memoir 48. Tulsa: American Association of Petroleum Geologists. pp. 239 – 248.
- [3]. Ekweozor, C. M. & Daukoru, E. M. (1994). Northern Delta Depobelt Portion of the Akata-Agbada Petroleum System, Niger Delta, Nigeria. In: Magoon, L. B. & Dow, W. G. Editions. *The Petroleum System from Source to Trap*. American Association of Petroleum Geologists Memoir 60. Tulsa: American Association of Petroleum Geologists, pp. 599 – 614.
- [4]. Gardner, G. H. F., Gardner, L. W. & Gregory, A. R. (1974). Formation Velocity and Density – the Diagnostic Basics for Stratigraphic Traps. *Geophysics*, 39: 770 – 780.
- [5]. George, N. J., Akpan, A. E., George, A. M. & Obot, I. B. (2010). Determination of Elastic Properties of the Over Burden Materials in Parts of Akamkpa, Southern Nigeria using Seismic Refraction Studies. *Archives of Physics Research*, 1(2): 58 – 71.
- [6]. Gray, F. D., Anderson, P. & Gunderson, J. (2006). Prediction of Shale Plugs between Wells in Heavy Oil Sands using Seismic Attribute. *Natural Resources Research*, 15(2): 102 – 109.
- [7]. Hospers, J. (1965). Gravity Field and Structure of the Niger Delta, Nigeria, West Africa. *Geological Society of American Bulletin*, 76: 407 – 422.
- [8]. Kaplan, A., Lusser, C. U. & Norton, I. O. (1994). *Tectonic Map of the World*. Tulsa: American Association of Petroleum Geologists.
- [9]. Kearey, P., Brooks, M. & Hill, I. (2002). *An Introduction to Geophysical Exploration*. Oxford: Blackwell Science.
- [10]. Koughnet, V. R. W., Skidmore, C. M., Kelly, M. C. & Lindsay, R. (2003). Prospecting with Density Cube. *The Leading Edge*, 22: 1038 – 1045.
- [11]. Kulke, H. (1995). *Regional Petroleum Geology of the World. Part II: Africa, America, Australia and Antarctica*. Berlin: Gebrüder Borntraeger. pp. 143 – 172.
- [12]. Lindseth, R. O. (1979). Synthetic Sonic Logs – a Process for Stratigraphic Interpretation. *Geophysics*, 44: 3 – 26.
- [13]. Quijada, M. F. & Stewart, R. R. (2007). Density Estimations using Density-Velocity Relations and Seismic Inversion. *CREWES Research Report*, 19:1 – 20.
- [14]. Tuttle, M. L. W., Charpentier, R. R. & Brownfield, M. E. (1999). *The Niger Delta Province, Nigeria, Cameroon and Equatorial Guinea, Africa*.
- [15]. Whiteman, A. (1982). *Nigeria: Its Petroleum Geology, Resources and Potential*. London: Graham and Trotman.

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