Mathematical Kinetic and Thermodynamic Study of Adsorption of Magnesium II by Alkaline Soil using Batch Method

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Abstract :

Clayal soil of study area with a pH of more than 8.5 are classified as alkaline soils. The higher pH is caused by high quantities of salt, magnesium and calcium. Further more hard water can cause the pH of soils to rise to alkaline proportions. Chemically the soil of CCA is rich in lime, iron, magnesium and alumina. In this way the aim of this work was to study the adsorption of Mg^{2+} on to the soil sample [ss] with different amount of adsorbate of particular ion salt $([Mg^{2+}]_{eff})_{MgCl_2}$ in the temperature range of 293K to 313K by using batch process method. Rate of adsorption was found nearest to Ist order reaction. Adsorption and desorption process run as complementary process gave equilibrium constant k_e which tends to give approach of thermodynamics parameters like enthalpy change, Gibbs free energy change, entropy changes respectively $[\Delta H^{\circ}], [\Delta G^{\circ}], [\Delta S^{\circ}]$ with the help of mathematical modeling the kinetics and thermodynamic parameter were interpreted to make ease to understood with clear predictions, distribution classification and assumptions of the entire data's mutual relation.

Key Words : Equilibrium Constant, Kinetic parameter, Enthalpy changes, Free energy changes, Entropy changes.

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1. Introduction

Abundance of magnesium is as equal as calcium which is a competitor ion of sodium and affect the NAR and directly to cation exchange capacity of other cations.^(1,2,3) Manual causes, climatic reasons or area specialties besides all physiochemical parameters affects the leaching kinetics and thermodynamics. ^(4,5,6) Alkali soils owe their unfavorable physicochemical properties mainly to the dominating presence of particular salt which causes the soil to swell and difficult to clarify or settle.⁽⁷⁻¹⁰⁾ Although magnesium plays important role in cation exchange capacity and because of its small size it is easily leached consequently affecting the quality of soil and ground water even surface water.^(11,12) So it was keened to study the magnesium leaching kinetics and thermodynamics factors to clarify the adsorption or desorption of ion having relation with cofactors like other counter ions, competitor ions, climatic or seasonally changes or temperature changes.^(5,6) A very abundant salt MgCl₂ was selected to study the adsorption or desorption process through the glass column method and using by batch process method. Using by batch process method various parameters studied in

a range of temperature $[T]_{293K}$, $[T]_{313K}$ by adding various amount of salt. In order to understand adsorption efficiency of sodium adsorption kinetic studies were done which describe residential or uptake time of solute on solvent at the solid solution interface^(4,5). The kinetical parameters can enhance to scaling up studies of soil remediation process connecting optimum operational conditions of magnesium predicting by important directional or nondirectional operations of the ion adsorption and remedial operations.^(6,7,8,9) As temperature can make two types effects on the adsorption process as physical adsorption and chemical adsorption process which are opposite qualities in the reference of increasing temperature. So only temperature changes are not sufficient parameter to determine the type of adsorption.⁽¹⁰⁾ Thus enthalpy change $[\Delta H^{\circ}]$ Gibbs free energy change $[\Delta G^{\circ}]$ and entropy change $[\Delta S^{\circ}]$ were too observed and calculated of each experiment to know whether the reactions are spontaneous or non spontaneous or feasible. $[\Delta G^{\circ}]$ was found negative⁽¹¹⁾ while $[\Delta H^{\circ}]$ was distinct positive⁽¹²⁾.

2. Material and Methods

For the estimation of magnesium $\left[Mg^{2+}\right]$ amount or concentration during adsorption or desorption process on the soil sample [SS], the soil sample were collected, dried and sieved for removing unwanted particles, from study region. Length 60cm and diameter of 3cm of glass column was prepared and gently packed or filled with 60gm soil. A fixed

amount of salt as effluent $\left(\left[Mg^{2^+} \right]_{eff} \right)_{MgCl_2}$ were added in the temperature range of $\begin{bmatrix} T \end{bmatrix}_{293K}$ to $\begin{bmatrix} T \end{bmatrix}_{313K}$ according to Rajasthan climate.

In thermostat conditional concentration change of $\left[Mg^{2+}\right]$ was noticed and with the help of adsorbed amount of sodium $[AC]_{ad}$ and unadsorbed amount of sodium $[AC]_{uad}$,

 $k_e = \frac{k_{ad}}{k_{uad}} = \frac{[AC]_{uad}}{[AC]_{ad}}$ were noticed for further kinetics and equilibrium constant $\left[\Delta H^{\circ}\right]$ by van't hoff equation $\frac{d\ln k}{dT} = \frac{\Delta H^{\circ}}{RT^2}$ thermodynamics studies enthalpy

 $\ln\left(\frac{k_2}{k_1}\right) = \frac{\Delta H^{\circ}}{8.314} \left(\frac{T_2 - T_1}{T_1 T_2}\right)$

Gibbs energy by the following equations

 $\Delta G^{\circ} = -RT$ $k_a \Delta S^{o}$ $k_e \Delta S^{\circ}$ ln , by the following equation $\Delta S^{\circ} = \frac{\Delta H^{\circ} - \Delta G^{\circ}}{T}$ were calculated consequently in order to know reaction feasibility or spontaneity.

The treatment of calculation of obtained data is based on the some parameter as defined below.

$$\begin{bmatrix} SS \end{bmatrix} = \text{Soil sample} \\ \begin{bmatrix} AC \end{bmatrix}_{ad} = \text{Concentration of } \begin{bmatrix} Mg^{2+} \end{bmatrix} \text{ adsorbed on adsorbent in mg.} \\ \begin{bmatrix} AC \end{bmatrix}_{uad} = \text{Concentration of } \begin{bmatrix} Mg^{2+} \end{bmatrix} \text{ unadsorbed on adsorbent in mg} \\ k_e \\ = \text{Equilibrium constant ie} \quad k_e = \frac{\begin{bmatrix} AC \end{bmatrix}_{uad}}{\begin{bmatrix} AC \end{bmatrix}_{ad}} \\ \end{bmatrix}$$

 $[T]_{293K}$ = Temperature of 293 K

maintained during experimental work in kelvin.

 $[T]_{313K}$ = Temperature of 313 K maintained during experimental work in kelvin.

 $\left(\left[Mg^{2^+}\right]_{eff}\right)_{MgCl_2}$ = Magnesium salt added from the top of glass column as effluent or adsorbate mg/gm

 $[\Delta H^{\circ}]_{293K-313K}$ = Enthalpy change with the temperature, change in kilo joul per mole $KJmol^{-1}$ $[\Delta G^{\circ}]_{293K-313K}$ = Gibbs free energy change with the temperature change in kilo joul per mole

 $KJmol^{-1}$.

 $[\Delta S^{\circ}]_{293K}$ = Entropy change with the 293 K temperature in joul per kelvin per mole $JK^{-1}mol^{-1}$

 $[\Delta S^{\circ}]_{313K}$ = Entropy change with the 313 K temperature in Joul per kelvin per mole $JK^{-1}mol^{-1}$ Table 1 : Determination of Kinetic and thermodynamic parameters k_e , $[\Delta H^{\circ}]_{293K-313K}$, $[\Delta G^{\circ}]_{293K-313K}$, $[\Delta S^{\circ}]_{293K}$, $[\Delta S^{\circ}]_{313K}$, with the addition of various amount of salt $([Mg^{2+}]_{eff})_{MgCl_2}$ as absorbate on the soil sample [SS] as the adsorbent in the range of temperature $[T]_{293K}$ and $[T]_{313K}$.

| $\left(\left[Mg^{2+}\right]_{eff}\right)_{M,GI}$ | $[k_{eq}]_{293K}$ | $[k_{eq}]_{^{313K}}$ | [ΔH°] _{293K-313K} | [ΔG°] _{293K-} | $[\Delta S^{\circ}]_{_{293K}}$ | [ΔS ^o] _{313K} |
|--|-------------------|------------------------------------|---|------------------------|--------------------------------|------------------------------------|
| (= -w / MgCl ₂ | | | | 313K | | |
| 58.14 | 8.21 | 5.92 | 9.66 | 13.05 | 19.50 | 18.30 |
| 78.12 | 4.13 | 34.08 | 9.58 | -7.29 | 51.90 | 48.65 |
| 98.20 | 2.64 | 4.33 | 9.54 | -3.28 | 38.05 | 35.6 |
| 118.22 | 2.10 | 3.08 | 9.83 | -2.61 | 36.79 | 34.50 |
| 139.28 | 1.84 | 2.44 | 9.92 | -1.67 | 33.80 | 31.71 |
| 159.31 | 1.69 | 2.11 | 10.11 | -2.12 | 36.03 | 33.81 |
| 178.34 | 1.58 | 1.91 | 10.12 | -2.01 | 36.62 | 34.36 |
| 199.01 | 1.51 | 1.78 | 10.1 | -1.91 | 36.22 | 33.97 |
| 218.11 | 1.43 | 1.67 | 10.32 | -1.83 | 35.6 | 33.55 |
| 238.42 | 1.41 | 1.59 | 10.46 | -1.77 | 36.06 | 33.81 |
| Mean | 2.654 | 5.891 | 9.964 | -1.144 | 36.057 | 33.826 |
| S.D. | 2.120 | 10.001 | 0.312 | 5.264 | 7.712 | 7.221 |
| R ² (linear) | 0.575 | 0.270 | 0.912 | 0.092 | 0.004 | 0.005 |
| \mathbb{R}^2 | 0.864 | 0.319 | 0.92 | 0.303 | 0.064 | 0.064 |
| (Polynomial) | | | | | | |
| <i>k</i> . | | $\begin{bmatrix} AC \end{bmatrix}$ | $\left(\begin{bmatrix} 1 & 2+ \end{bmatrix} \right)$ | | | |

 $k_{e} = \frac{[AC]_{uad}}{[AC]_{ad}} * \left([Mg^{2+}]_{eff} \right)_{MgCl_{2}} \text{ Adsorbate in mg/gm}$ $* [\Delta H^{\circ}]_{293K-313K} \text{ Enthalpy change in } KJ \ mol^{-1} * [\Delta G^{\circ}]_{293K-313K} \text{ Gibbs free energy change in } KJ \ mol^{-1} * [\Delta S^{\circ}]_{293K} \text{ Entropy change in } JK^{-1}mol^{-1} \text{ at } 293 \text{ K} * [\Delta S^{\circ}]_{313K} \text{ Entropy change in } JK^{-1}mol^{-1} \text{ at } 313 \text{ K}$

Figure 1 : Mathematical modeling and determination of kinetic and thermodynamic parameters k_e , $[\Delta H^\circ]_{293K-313K}$, $[\Delta G^\circ]_{293K-313K}$, $[\Delta S^\circ]_{293K}$, $[\Delta S^\circ]_{313K}$, with the addition of $\left(\left[Mg^{2+}\right]_{eff}\right)_{MgCl_2}$ as absorbate on the soil sample [SS] as the adsorbent various amount of salt in the range of temperature $[T]_{293K}$ and $[T]_{313K}$.



Figure 2 : Mathematical modeling and determination of kinetic and thermodynamic parameters k_e , $[\Delta H^\circ]_{293K-313K}$, $[\Delta G^\circ]_{293K-313K}$, $[\Delta S^\circ]_{293K}$, $[\Delta S^\circ]_{313K}$, with the addition of various amount of salt $\left(\left[Mg^{2+} \right] \right)$ $\int_{eff} \int_{MgCl_2}$ as absorbate on the soil sample as the adsorbent in



the range of temperature $[T]_{293K}$ and $[T]_{313K}$.

3. Result and Discussion

Very interesting results were obtained during entire work process of adsorption of magnesium II during a temperature range with changing in adsorbate quantity. Equilibrium constant k_e were calculated of each experiment and further Gibbs free energy $[\Delta G^{\circ}]$ calculated on the behalf. Negative values of $\left[\Delta G^{\circ}\right]$ indicate reaction during magnesium II ions adsorption is how much spontaneous process. With increasing temperature adsorption was too found in increasing order as particles potential energy too increases thus enthalpy changes were too noticed increasing because of endothermic reaction entropy changes were observed positive which indicate the randomness of unadsorbed part and slightly increasing of adsorbed part ratio. It is well known absolute. Entropy is not inversely proportional to absolute temperature which increases with temperature because of increasing atomic vibration and the disorder of system but change in entropy in a constant temperature heat transfer does make it seems like entropy is inversely proportional to temperature based on the equation, but it actually only means that the amount of entropy change is less at higher temperature for a given heat transfer according to formulae $\Delta S^{\circ} = Q/T$ if $\Delta S^{\circ} = \Delta H^{\circ} - \Delta G^{\circ}/T$. Mathematical modelling proves closeness of data to actual theory and equations.

The positive values of mean observed as 2.654 for $[k_{eq}]_{293K}$, 5.891 for $[k_{eq}]_{313K}$, 9.964 for $[\Delta H^{\circ}]_{293K-313K}$, 36.057 for $[\Delta S^{\circ}]_{293K}$, 33.826 for $[\Delta S^{\circ}]_{313K}$ and negative value -0.153 for $[\Delta S^{\circ}]_{293K-313K}$ were observed while SD as 2.120, 10.001, 0.312, 5.264, 7.712, 7.221 R^2 (linear) as 0.575, 0.270, 0.912, 0.092, 0.004, 0.005 R^2 (Polynomial) as 0.864, 0.319, 0.921, 0.303, 0.064, 0.064 for $[k_{eq}]_{293K}$, $[k_{eq}]_{313K}$, $[\Delta H^{\circ}]_{293K-313K}$, $[\Delta G^{\circ}]_{293K-313K}$, $[\Delta S^{\circ}]_{293K}$, $[\Delta S^{\circ}]_{313K}$, respectively shows closeness to actual data.

4. Conclusion

The abundant magnesium salt affected by CAC process and leaching V/s adsorption mechanism the entire process of thermodynamic and kinetics studies of adsorption of ion may help to know ion adsorption and leaching efficiency in the soil medium in order to know retain or escaping capacities of metals in the soil and their contamination boundaries.

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